Effect of depolarization and coercivity on actuation strains due to domain switching in barium titanate

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Large electrostrictive actuation in ferroelectric single crystals can be achieved through non-180° domain switching using various biasing fields and loads. The theoretical maximum actuation strain such as 1.1% for barium titanate crystals, however, has not been observed yet. In this letter, the authors propose a possible mechanism accounting for the depolarization effect to explain the significant strain reduction observed in their recent experiment. They find that a low-energy path requires the switching of 90° domains together with that of in-plane alternating layers of 180° domains formed to reduce the depolarization energy. Therefore, reduction in strain is significant for crystals with large 180° coercivities. The result is consistent with their recent experimental observations. © 2007 American Institute of Physics. [DOI: 10.1063/1.2731315]

The interest in large strain actuation has motivated many experimental efforts using ferroelectric single crystals to achieve this goal. A variety of attempts has been carried out by inducing large changes in the polarization orientation either via phase transition or via domain switching. Park and Shrout utilized the phase transition to obtain “ultrahigh strain” in a single crystal relaxor ferroelectric PZN-PT (a solid solution of lead zirconate niobate and lead titanate) which possesses an electrostrictive strain up to 1.7% at around 10 MV m⁻¹.¹ Ren demonstrated that the symmetry-conforming property of point defects can give rise to strain up to 0.75% at 0.2 MV m⁻¹ in thermally aged barium titanate (BaTiO₃) crystals.² Burcsu *et al.* examined the 90°-switching-induced strain of BaTiO₃ crystals under a combined electrical and mechanical loading, and observed nearly 0.8% strain at 1.78 MPa compressive stress together with 1 MV m⁻¹ electric field.^{3,4} However, the maximum actuation strain allowed by crystallography, such as 1.1% predicted for BaTiO₃ single crystals,⁵ has not been observed yet. This has motivated a number of research efforts to study the switching mechanism experimentally and theoretically.⁶⁻⁹ In particular, since large strain behavior caused by domain switching is typically induced through angles other than 180°, it is therefore essential to investigate factors which might influence the “effectiveness” of non-180° switchings. Shilo *et al.* have recently proposed a switching model to explain the strain reduction found in the experimental work of Burcsu *et al.*¹⁰ Their model has assumed the existence of friction between the ferroelectric crystal and the loading device, showing that the strain is reduced due to this factor. The current investigation, on the other hand, focuses on another possible mechanism accounting for the depolarization effect for the switching hardening.

Consider a ferroelectric single crystal described by two state variables: strain ϵ and polarization $\mathbf{p}$. The reduction in crystal symmetry from the paraelectric to the ferroelectric

phase implies that the ferroelectric crystal has several ground states (variants) in the strain-polarization space. For BaTiO₃ in the tetragonal phase, there exist six possible variants with the polarization vector in one of the six pseudocubic $\langle 100 \rangle$ directions, and the different variants can coexist as “domains” in very intricate and characteristic patterns: the underlying distortion must be continuous and the interface must be uncharged. A detailed classification of domain patterns in ferroelectric crystals has been explored by Shu and Bhattacharya,⁵ and their analysis suggests that there exists a low-energy path for switching from one polarization to another by a combined electrical and mechanical loading. Indeed, for a flat-plate configuration with electrodes on the top and bottom surfaces, the potential energy per unit volume of the system in the two-dimensional (2D) version of the framework⁵ can be written as

$$\langle I \rangle = -E_3^* \langle p_3 \rangle - \sigma_{33}^* \langle \epsilon_{33} \rangle + \frac{C}{2\epsilon_0} \langle p_1 \rangle^2, \quad (1)$$

where $\langle \cdots \rangle$ stands for the volume average, E_3^* and σ_{33}^* are the applied electric field and stress, ϵ_0 the permittivity of free space, and C is a constant related to the geometry of the crystal. Several comments for Eq. (1) are made here. First, the last term of Eq. (1) is the contribution of the depolarization energy. For a rectangular geometry with thickness H and length L , $C \approx 8(H/L) \sum_{n=1}^{\infty} [1 - (-1)^n] / n^3 \pi^3 (1 - e^{-n\pi(L/H)})$. Therefore, unless the ratio H/L is extremely small, the effect of depolarization energy may *not* be neglected. Second, Eq. (1) has no contribution from the depolarization in the interior since the domain patterns are assumed to be compatible.¹¹ Third, while there are various candidates of domains which can be chosen for Eq. (1), an important one is a multirank laminate. For example, rank-1 lamellar and rank-2 banded domains are commonly observed patterns in BaTiO₃.^{12,13} Further, it has been shown that, given an arbitrary average state of strain and polarization, a minimum energy configuration of domains can be constructed through multirank lamination.¹⁴⁻¹⁶ Based on this result, the lowest rank laminate satisfying the above property in a 2D tetragonal BaTiO₃

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FIG. 1. Compatible domain pattern using rank-3 lamination in a BaTiO₃ single crystal. Notice that the change in the local volume fraction μ_1 induces two types of domain wall movements.

crystal is a three-rank compatible domain pattern as illustrated in Fig. 1. The polarization and strain averages of this pattern are given by

$$\langle p_1 \rangle = [\mu_1 - (1 - \mu_1)\mu_2]P_s,$$

$$\langle p_3 \rangle = (1 - \mu_1)(1 - \mu_2)(2\mu_3 - 1)P_s, \quad (2)$$

$$\langle \epsilon_{33} \rangle = \eta_1 + (\eta_2 - \eta_1)[\mu_1 + (1 - \mu_1)\mu_2], \quad (3)$$

where $\eta_1 = 0.67\%$, $\eta_2 = -0.42\%$, and $P_s = 0.26 \text{ C m}^{-2}$ are measured parameters for spontaneous strain and polarization,¹⁷ and μ_1 , μ_2 , and μ_3 denote the local volume fractions appearing in the first, second, and third ranks, respectively.

The reduction in potential energy provides the (thermodynamic) driving force for the domain evolution. However, switching is resisted by the dissipative motion of domain walls,⁷ and as a result, domain switching occurs when

$$\frac{\partial}{\partial \mu_i} \langle I \rangle(\boldsymbol{\mu}) d\mu_i + G_i^c(\boldsymbol{\mu}) |d\mu_i| \leq 0, \quad (4)$$

where $G_i^c(\boldsymbol{\mu})$ is the critical dissipative energy density and is explained as follows. Assume that volume fractions μ_2 and μ_3 shown in Fig. 1 are fixed. The change in μ_1 will involve two types of domain wall movements: 180° wall motion in the region with local volume fraction μ_2 and 90° wall motion in another region with local volume fraction $(1 - \mu_2)$. Let

FIG. 2. Schematic of the combined electromechanical loading apparatus.

FIG. 3. Experimental observations of maximum actuation strains from three different BaTiO₃ single crystals (labeled C, M, and S) under combined electrical and mechanical loadings.

E_{180}^c and E_{90}^c denote the coercive electric fields necessary to move 180° and 90° domain walls in tetragonal crystals, respectively. The dissipation energy density due to the change in μ_1 is therefore

$$\begin{aligned} G_1^c(\boldsymbol{\mu}) &= (\mathbf{E}_{180}^c \cdot \Delta \mathbf{p})\mu_2 + (\mathbf{E}_{90}^c \cdot \Delta \mathbf{p})(1 - \mu_2) \\ &= 2P_s E_{180}^c \mu_2 + P_s E_{90}^c (1 - \mu_2). \end{aligned} \quad (5)$$

Other explicit expressions of $G_2^c(\boldsymbol{\mu})$ and $G_3^c(\boldsymbol{\mu})$ can also be derived in a similar way with a different competition between E_{180}^c and E_{90}^c .

From Eq. (4), the switching starts when the applied electric field and stress reach the values determined by

$$-P_s E_3^* + (\eta_2 - \eta_1)\sigma_{33}^* + \frac{C}{\epsilon_0} P_s \langle p_1 \rangle = P_s E_{90}^c. \quad (6)$$

Notice that if the depolarization effect is not taken into account, i.e., $C=0$ in Eq. (6), the 90° switching process would

FIG. 4. Simulations of actuation strains in comparison with experimental observations in Fig. 3.

be completed if the electromechanical loading is balanced by the coercive field $P_s E_{90^\circ}^c$, and therefore, the actuation strain would achieve its maximum value $\eta_1 - \eta_2$. If, however, $C \neq 0$ in Eq. (6), the switching depends on $\langle p_1 \rangle$ which is related to the local volume fractions μ_1 and μ_2 by Eq. (2). The amount of μ_2 can be determined by

$$-P_s E_3^* + (\eta_2 - \eta_1) \sigma_{33}^* = P_s E_{90^\circ}^c + P_s E_{180^\circ}^c \mu_2, \quad (7)$$

and μ_1 is solved from Eq. (6). Physically, as illustrated in Fig. 1, the in-plane alternating layers of 180° domains are formed to reduce the depolarization energy. The compatibility in domain structure requires that the change in μ_1 induces both the 90° and 180° switchings. Therefore, large coercive field $E_{180^\circ}^c$ implies a significant amount of energy dissipated in moving these in-plane layered domains, which in turn is not favorable for the 90° switching process. Indeed, from Eq. (7), larger $E_{180^\circ}^c$ gives rise to smaller μ_2 at the same level of applied field and stress, resulting in smaller strain in actuation.

The theoretical framework described above is developed to explain a series of experiments for measuring actuation strains of BaTiO₃ single crystals under combined electrical and mechanical loadings. (001)-oriented cuboidal BaTiO₃ single crystals measuring $5 \times 5 \times 2$ mm³ were obtained from MTI Corp., CA (labeled M) and Superconix Inc., MN (labeled S). Conductive silver paint was used to produce electrodes on the 5×5 mm² faces. A loading fixture shown in Fig. 2 was developed for the simultaneous application of compressive stress and electric field. The mechanical and electrical loadings were supplied by a universal test frame and a high-voltage amplifier, respectively. Miniature strain gauges were attached onto the 5×2 mm² faces of the crystal to measure strain changes in the loading direction. Besides the strain measurements, the two input parameters required for the theoretical framework, $E_{180^\circ}^c$ and $E_{90^\circ}^c$ of the single crystal, were obtained, respectively, from the polarization hysteresis at zero compressive stress and from the *in situ* domain observation using crossed polarizers under an arrangement where the applied electric field was perpendicular to the poling direction of the polished crystal.

Upon the application of combined loadings, the maximum actuation strains produced by different BaTiO₃ single crystals are shown in Fig. 3 in the form of largest strain hysteresis (i.e., butterfly) curves. Figure 3 also displays the experimental strain data of the single crystal of Burcsu *et al.* (labeled C).⁴ It is found from Fig. 3 that crystals M and S exhibit more squashed and broadened butterfly curves and

significantly lower strain outputs in comparison with crystal C. Indeed, the measured strains for crystals M and S are about 0.4% while crystal C produced a strain close to 0.8%. To explain this, the butterfly loops are simulated using Eq. (4) as well as the coercive fields measured independently from Fig. 3. The $E_{180^\circ}^c$ is about 0.2–0.3 MV m⁻¹ for crystals M and S while $E_{180^\circ}^c \approx 0.04$ MV m⁻¹ for crystal C. The $E_{90^\circ}^c$ is around the same level of $E_{180^\circ}^c$ for each crystal. Notice that the coercive fields for crystals M and S are almost one order of magnitude larger than those for crystal C. Simulations of the actuation strains of these three crystals are shown in Fig. 4. It is evident that the developed framework is capable of explaining the wide differences in electrostrictive behaviors as shown in Fig. 3.

In summary, a framework is developed to predict the strain hysteresis of barium titanate single crystals under combined electric field and stress. It is shown that the depolarization and coercivities have a nontrivial effect on the attainable actuation strain.

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