Morphology and growth rate of calcium carbonate crystals in a gas–liquid–solid reactive crystallizer

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Abstract—The polymorphism of calcium carbonate crystal was studied by introducing CO₂ gas through a gas sparger or a double-tube gas injection nozzle into a pH-stat crystallizer containing calcium chloride solution. Several operating variables were investigated and the pH of solution and calcium ion concentration were the important factors that affect the formation of polymorphs of calcium carbonate. At ambient temperature either calcite or vaterite was the major product, depending on the pH and calcium ion concentration. Then the same crystallization system was employed to study the growth kinetics of calcite crystals, using a double-tube gas injection nozzle instead of a gas sparger, which cannot be used to suppress nucleation, to introduce the CO₂ gas into the crystallizer. The growth rates of calcite seeds increased with increasing supersaturation and crystal size. As a conclusion, the polymorphs and growth rate of calcium carbonate are controllable in a gas–liquid–solid reactive crystallizer, using a pH-stat operation mode. © 1997 Elsevier Science Ltd

Keywords: Polymorphism; calcium carbonate; crystal growth; gas–liquid–solid system; two-step growth model; induction period.

I. INTRODUCTION

Calcium carbonate is a widely used chemical in various industries and an abundant compound found in the nature. The crystallization phenomena of this sparingly soluble salt are very complicated because it precipitates in three crystalline forms, including calcite, aragonite, and vaterite, and the operating variables, such as the pH of solution, solution composition, temperature, and ionic strength, are interrelated and interact on each other in a crystallization process.

The liquid–liquid–solid reactive processes are often adopted in a laboratory study because of its simplicity in the operation or its easiness in the control of process variables. For example, Wray and Daniels (1957) investigated the polymorphs of calcium carbonate precipitates by mixing soluble carbonate solutions with solutions of calcium ions under conditions of controlled temperature, concentration, and aging; Sohnel and Mullin (1982) determined the growth rate of crystals by a desupersaturation method and explored the effects of impurities on crystal morphology; Hostomsky and Jones (1991) found that the crystal form was dependent on the residence time, pH, and the concentration of reagents in an MSMPR crystallizer; Tai et al. (1993) and Koutsoukos (1993) studied the growth kinetics and morphology using a pH-stat method; Tai et al. (1995) and Wojcik and Jones (1997) investigated the dynamic and kinetic behaviors in the agglomeration process of CaCO₃ precipitates; and Isopescu et al. (1996) analyzed the crystallization data based on the size-dependent growth model. However, the precipitated calcium carbonate are produced commercially by passing carbon dioxide through a milk of lime, i.e. by a gas–liquid–solid reacting method. Studies on gas liquid solid systems are rare because the process variables are interrelated and are difficult to control as compared with the liquid–liquid–solid systems. The report by Yagi et al. (1984) was perhaps the first one to systematically study the three-phase system. However, the crystallizer used was a stirred vessel with a flat gas–liquid interface, which has no practical use. Besides, there was no control of the pH of solution during the course of precipitation. Jones and his coworkers (Wachi and Jones, 1991; Jones et al., 1992) continued to perform similar experiments and
modeled the crystal size distribution of CaCO₃ precipitates with some degree of success. Kojima et al. (1992) studied the crystal morphology of calcium carbonate which was precipitated by outgassing dissolved CO₂ in calcium hydrogen carbonate solution. Although the pH of solution was not controlled during the precipitation process, they were able to produce rhombohedral-like calcite, prismatic-like aragonite, and hexagonal plate-like vaterite with the initial pH of solution varying between 6.2 and 8.0 and the temperature between 20 and 100°C.

In our laboratory a gas-liquid-solid reactive crystallizer was employed to study the polymorphs of calcium carbonate and the growth rate of calcite crystal, which is the thermodynamically stable form of calcium carbonate at atmospheric pressure and ambient temperature. The CO₂ gas was introduced into the crystallizer, in which the concentration of hydrogen ion was maintained at a constant level by using a pH-stat apparatus, through a double-tube injection nozzle or a gas sparger. Several process variables, including the pH of solution, concentration of calcium ion, concentration ratio of [HCO₃⁻]/[CO₃²⁻], and gas liquid mixing mode were investigated. The results on the polymorphs of calcium carbonate and the crystal growth kinetics of calcite were compared with those obtained from the liquid-liquid-solid systems.

2. EXPERIMENTAL

A schematic diagram of the semibatch crystallization apparatus is shown in Fig. 1. It consists of a pH-stat autotitrator (Kyoto Electronic AT 200), an ion meter (Orion EA 920), a 1.5l acrylic crystallizer, a constant-temperature water bath, and a double-tube gas injection nozzle or a gas sparger. The diameter and height of the crystallizer, fitted with four baffles at 90° spacing, are 120 and 140 mm, respectively. The construction of the double-tube gas injection nozzle followed the design of Kubota et al. (1990) as shown in Fig. 2. The advantage of this design is to avoid nucleation in the outer tube, where CO₂ gas contacts with solution bearing a low pH. The pH of solution was measured by means of a pair of glass (Kyoto Electronic H-112) and reference (Kyoto Electronic R-116) electrodes, standardized before each experiment with standard buffers of pH 6.86 and 9.18. The CO₂ gas dissolved in solution as carbonates was measured by a CO₂-electrode (Orion Research), which was calibrated with a standard solution of sodium carbonate. All the experiments were conducted at 30°C.

The experiments were first performed for the study of crystal morphology. A solution of desired concentration was prepared using the calcium chloride crystals as received (Merck, EP Grade) and deionized water. After being filtered, 1 l of solution was transferred to the crystallizer with the impeller running at 600 rpm, which is high enough to suspend CaCO₃ crystals in all experiments conducted in this study. Then the pH of solution was adjusted to a desired value by adding drops of 0.1 M KOH solution. After the pH became steady, we opened the regulator of CO₂ gas cylinder and let the CO₂ gas flow through the injection nozzle to contact with the solution. The pH of solution was maintained at a constant level during the operation by constantly adding KOH solution, which was controlled by the autotitrator. The concentration of solution was kept in the labile region, where the supersaturation is so high that the primary nucleation would occur to produce nuclei, of a precipitation diagram which was plotted previously (Chen, 1995) and was shown in Fig. 3. The calcium carbonate was precipitated after an induction period, and the operating time varied from 30 to 100 min, depending on the production rate of precipitates. In the course of reactive precipitation, a solution of 2.5 ml was withdrawn from the crystallizer every 3 min and was filtered with a 0.22 μm membrane to remove solid particles for subsequent analysis of Ca²⁺ concentration using the atomic absorption method. Finally, after the precipitated particles were filtered and dried, the morphology of precipitates was examined by a scanning electron microscope and the fraction of polymorphs was determined by a X-ray powder diffractometer.

The experimental procedures in the crystal growth study were somewhat different from that of morphology study. A certain amount of calcite seeds were added to the crystallizer after the pH of solution became steady. Besides, the flow of CO₂ gas was
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3. Determination of Relative Supersaturation and Crystal Growth Rate

3.1. Relative supersaturation

The relative supersaturation, $\sigma$, used in this work was defined by Nielsen and Toft (1984):

$$\sigma = \left( \frac{\Pi}{K_{sp}} \right)^{1/2} - 1$$

where $\Pi$ is the ionic product and $K_{sp}$ is the solubility product. When the pH of solution, total calcium ion concentration, total carbonate concentration, and activity coefficient equation were known, the concentrations of ionic species were calculated by the method of successive approximation for the ionic strength (Nancollas, 1966; Tai et al., 1993).

3.2. Determination of crystal growth rate

The mass growth rate per unit surface area of crystal can be expressed as follows:

$$\frac{1}{A} \frac{dm}{dt} = \frac{\rho_s}{A} \frac{dV}{dt} = \frac{3\rho_s f_s}{f_s} \frac{4L}{dt}$$

where $A$, $V$, and $\rho_s$ are the surface area, volume, and density of seed crystals, respectively. The linear growth rate is related to the mass growth rate by the following equation,

$$G = \frac{dL}{dt} = \frac{f_s}{3f_s \rho_s A} \frac{dm}{dt}$$

where mass growth rate, $dm/dt$, can be estimated from the depletion of calcium ion.

$$\frac{dm}{dt} = MV \left( - \frac{d[Ca^{2+}]}{dt} \right)$$

where $M$ is the molecular weight of calcium carbonate, $V$ the volume of solution, and $[Ca^{2+}]$ the molar concentration of calcium ion. Because the crystal form of calcite is rhombohedron, the value of $J_s^*:3f_s$ is close to 2. Substituting this value and eq. (4) into eq. (3), the linear growth rate becomes:

$$G = \frac{dL}{dt} = \frac{2MV}{\rho_s A} \left( - \frac{d[Ca^{2+}]}{dt} \right)$$

Equation (5) describes the linear growth rate as a function of calcium ion concentration. Once the concentration profile of calcium ion is available, the linear growth rate can be calculated at any instance of an experiment.

3.3. Growth rate model

Although the crystal growth rates may be influenced simultaneously by two or more mechanisms, the two-step model is commonly used to express a growth process as follows:

$$G = K_d(\sigma - \sigma_c) = K_{eq}L^* (\sigma - \sigma_c)$$

bulk diffusion

$$- K_{ss} \sigma_c' = K_{rr}L^* \sigma_c'$$

surface integration.
Combining eqs (6) and (7) by eliminating \( \theta_i \), the resultant equation is

\[
\sigma = \frac{G}{K_{eq} L^a} + \left( \frac{G}{K_{eq} L^b} \right)^{1/r}.
\]

(8)

Parameters \( a, b, K_{eq} \), and \( K_{eq} \) in eq. (8) can be evaluated by a nonlinear regression method for a given value of \( r \), when the supersaturation and growth rate data are available.

4. RESULTS AND DISCUSSION

4.1. Supersaturation and induction period

During the course of precipitation the supersaturation varied with time due to the accumulation or depletion of constituents. Figure 4 shows the change of relative supersaturation for various levels of pH under a constant flow rate of CO\(_2\) gas. All the curves in Fig. 4 exhibit a maximum, which approximately corresponds to the induction period because the decrease in supersaturation was caused by the commencement of nucleation. Therefore, the induction period of higher pH was shorter than that of lower pH. Besides, two different shapes of supersaturation curves are observed in Fig. 4; the changes in supersaturation for lower pH were moderate as compared with that of higher pH. The possible reasons are given below. The absorption rate of CO\(_2\) was higher at higher pH (Sherwood et al., 1975; Butler, 1982) so that the supersaturation increased sharply for higher pH, starting with approximately the same Ca\(^{2+}\) concentration for all levels of pH. Then, high nucleation rate at high supersaturation gave a quick drop in supersaturation.

4.2. Polymorphs of calcium carbonate

Thirty-three runs of experiment were conducted in this work to study the polymorphs of calcium carbonate. The percentage of polymorphs produced and the operating conditions are listed in Table 1. The pH range investigated was between 7.8 and 9.4. When the pH is lower than 7.8, the amount of precipitates produced was small. On the other hand, the control of the pH was difficult at higher pH. The carbonate ion concentration and bicarbonate ion concentration were calculated at the highest relative supersaturation, \( \sigma_m \). Then the ratio of bicarbonate ion concentration to carbonate ion concentration, \( \sigma_w \), was plotted against calcium ion concentration for different values of pH as shown in Fig. 5. It is surprising to see that the \( \sigma_w \) value decreases with increasing Ca\(^{2+}\) concentration at lower pH values. Under our operating conditions, the pH of solution is the most important factor that influences the formation of polymorphs of calcium carbonate. Nearly, pure products of vaterite were produced at pH below 8.0. The concentration of calcium ion seems to be a minor factor in the determination of vaterite. This result is contradictory to that reported by Yagi et al. (1984). They found that vaterites were produced at low Ca\(^{2+}\) concentration (< 0.4 mM). However, the pH of solution was not measured in their experiments. The maximum yield of calcites occurs somewhere around the pH of 8.6 for each series of experiment at a specified range of calcium ion concentration. This result is similar to that reported by Hostomsky and Jones (1991), who found that the maximum yield for calcite appeared at a pH of 8.5. The yield of calcite is also related to calcium ion concentration and gas dispersion method. The yield is highest for run 24, which has a high Ca\(^{2+}\) concentration (15.9 mM). The results are consistent with that reported by Yagi et al. (1984) and Wachi and Jones (1991). When the CO\(_2\) gas was introduced into the crystallizer through a gas sparger in the experimental series I and II, the yield of calcite at a similar calcium ion concentration is higher than that of the experiments (series III and V) using the double-tube gas injection nozzle. As for aragonite, a small amount was produced at 30°C for high pH and calcium ion concentration irrespective of the gas-dispersion method.

4.3. Growth rate of calcite crystals

In the growth rate study, the CO\(_2\) gas was introduced to the crystallizer through the double-tube injection nozzle. When a gas sparger was used, the suppress of nucleation in the crystallizer was not successful. Therefore, a comparison of growth-rate data between the two modes of gas dispersion is impossible. Growth rate of calcite crystals were estimated by eq. (5) using the slope of Ca\(^{2+}\) concentration profile, which is shown in Fig. 6 for three typical runs. In principle, growth rate of any instance can be obtained from a \([\text{Ca}^{2+}] - t\) curve. Actually, the growth rates were calculated at a time interval of 10 or 20 min, depending on the steepness of \([\text{Ca}^{2+}] - t\) curve. The
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Table I. Crystal polymorphs of calcium carbonate at various operating conditions

<table>
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<tr>
<th>Series no.</th>
<th>Run no.</th>
<th>[Ca(^{2+})] (mM)</th>
<th>pH</th>
<th>[HCO(_3)(^{-})] (mM)</th>
<th>[CO(_3)(^{2-})] (mM)</th>
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V: Vaterite; C: Calcite; A: Aragonite

The crystal growth data of the seeds of various sizes were plotted against the relative supersaturation as shown in Fig. 7. The crystal growth rates increase with increasing supersaturation and crystal size. Using the two-step growth model, the parameters in eq. (8) were estimated by a nonlinear regression method for smaller crystal sizes, including 20, 68 and 163 μm. The growth-rate data of larger sizes were excluded in the analysis because the increase in growth rate was not significant.

The regressed growth-rate equation is presented as follows.

\[
G = 5.54 \times 10^{-9} L^{0.86} (\sigma - \sigma_i) \quad (9)
\]

\[
= 4.40 \times 10^{-11} L^{0.20} \sigma_i^{2.90}. \quad (10)
\]

The mass-transfer and surface-integration rates are related to crystal size. This kinetic behaviors are commonly observed in crystal growth processes (Tai et al., 1993). The kinetic order of surface integration step is 2.9, which is higher than 2 found in a liquid-liquid reacting system (Tai et al., 1993) and is close to 3.0 reported by Qiu and Rasmuson (1990) for succinic acid.

Once the parameters in the growth-rate model are known, the controlling step of growth process can be judged by the effectiveness factor proposed by Garside (1971). The surface-integration effectiveness factor for an rth-order process is

\[
\eta = (1 - \eta Da)^{-1/\alpha} \quad (11)
\]

where

\[
Da = K_{rot} L^{-\alpha} \sigma^{-1/\alpha} \text{Da}. \quad (12)
\]

Equation (11) is plotted in Fig. 8. Since \(\eta\) approaches 1, the growth process is controlled by surface
integration. The result is consistent with many reports (Nancollas and Reddy, 1971; Kazmierczak et al., 1982; Christoffersen and Christoffersen, 1990) for the growth of calcite.

5. CONCLUSIONS
A gas–liquid–solid reactive crystallizer was successfully operated under the condition of constant pH to study the formation of polymorphs of calcium carbonate and crystal growth of calcite. In the polymorph study the CO₂ was introduced into the crystallizer by a gas sparger or a double-tube injection nozzle; however, the gas sparger cannot be used in the crystal growth study. Among the operating variables investigated in this study, the pH of solution and calcium ion concentration are the important factors that determine the polymorphs of calcium carbonate. When operated at 30°C, nearly pure products of vaterite are produced at pH below 8.0 in spite of the gas-dispersion method. The maximum yield of calcite occurs somewhere around the pH of 8.6. The yield of calcite is also influenced by the calcium ion concentration and gas-dispersion method. High concentration of calcium ion favors the formation of calcite. The aragonite is a minor product at 30°C. The crystal growth rate of calcite seeds increases with increasing supersaturation and crystal size, and the crystal growth process is controlled by surface integration.
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Acknowledgment
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NOTATION

- $a$: exponent of crystal size in eq. (6)
- $A$: specific surface area, m$^2$
- $b$: exponent of crystal size in eq. (7)
- $Cr$: ratio of $[\text{HCO}_3^-]$ to $[\text{CO}_3^{2-}]
- $Da$: Damkohler number
- $f_s$: surface shape factor
- $f_v$: volume shape factor
- $G$: linear growth rate, m/s
- $K_d$: mass-transfer coefficient, m/s
- $K_n$: surface-integration coefficient, m/s
- $K_{sp}$: solubility product
- $L$: crystal size, m
- $M$: molecular weight, kg/kg mole
- $m$: crystal mass, kg
- $R_d$: mass growth rate, kg/m$^2$s
- $r$: surface-reaction order
- $t$: time, min
- $V$: volume of solution, m$^3$
- $V_c$: volume of crystal, m$^3$

Greek letters

- $\sigma$: relative supersaturation
- $\sigma_i$: interfacial relative supersaturation
- $\rho_s$: density, kg/m$^3$
- $\eta$: surface-integration effectiveness factor
- $\Pi$: ionic product

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