Phase-Noise Reduction of X -Band Push–Push Oscillator With Second-Harmonic Self-Injection Techniques

To-Po Wang, *Student Member, IEEE*, Zuo-Min Tsai, *Student Member, IEEE*, Kuo-Jung Sun, and Huei Wang, *Fellow, IEEE*

Abstract—A low phase-noise X -band push–push oscillator using proposed feedback topology is presented in this paper. The oscillator core was implemented in a $0.18\text{-}\mu\text{m}$ CMOS process. By using a power splitter and a delay path in the feedback loop connecting the output and current source of the oscillator, a part of the oscillator output power injects to the oscillator itself. With the proper phase delay in the feedback loop and high transconductance of the current source, a low phase-noise oscillator is achieved. The amplitude stability and phase stability are analyzed, the phenomena of the phase-noise reductions are derived, and the device-size selections of the oscillator are investigated. The time-variant function, impulse sensitivity function, is also adopted to analyze the phase-noise reductions of the second-harmonic self-injected push–push oscillator. These theories are verified by the experiments. This self-injected push–push oscillator achieves low phase noise of -120.1 dBc/Hz at 1-MHz offset from the 9.6-GHz carrier. The power consumption is 13.8 mW from a 1.0-V supply voltage. The figure-of-merit of the oscillator is -188.3 dBc/Hz . It is also the first attempt to analyze the second-harmonic self-injected push–push oscillator.

Index Terms—Current source, delay line, figure-of-merit, high- Q resonator, self-injection.

I. INTRODUCTION

THE increasing demands on wireless data communication have motivated the development of RF front-end circuits toward tens of gigahertz. Being a crucial component in wireless systems, voltage-controlled oscillators (VCOs) impose restrictions on both active and passive devices for the technology of choice. As the CMOS feature size advances to deep sub-micrometer, CMOS fundamental oscillators at frequencies up to millimeter-wave range were reported [1], [2]. However, it usually requires expensive process technology, while delivering low output power. In order to implement low-cost oscillators for high-frequency applications, a cross-coupled push–push oscillator using a $0.25\text{-}\mu\text{m}$ CMOS technology was proposed to achieve an output frequency twice as high as the fundamental frequency with good fundamental rejection, even though the output frequency is higher than the f_{max} of the transistors [3]–[5]. Though demonstrating high oscillating frequency and

acceptable output power, the push–push VCO phase noise is usually limited due to lack of high- Q on-chip inductors.

To overcome the poor phase noise in a free-running oscillator, low phase-noise oscillators usually use the high- Q resonators to stabilize the oscillating signals for reducing the noise components [6]–[9]. With a high- Q factor, the VCO will be more stable because the phase fluctuation and frequency fluctuation approximate zero. Injection lock with external stable signal source is another technique used in Si-based circuit design such as frequency dividers [10]–[12] and quadrature generation [13]. With an external injection low-noise signal, the locking range and phase noise of the injection-locked oscillator is associated with the injection signal strength and the Q factor of the resonator of the VCO. The larger the injection signal amplitude, the wider the locking range, and the better the phase noise will be.

The feedback-loop technique is applied in lasers [14], [15] or used to stabilize the oscillators [16]–[18]. The regular self-injection-locked oscillator [19]–[21] is shown in Fig. 1(a) where the self-injection signal has the same frequency as the oscillator. The oscillator output signal goes through the circulator, and then into the input port of the power divider. Part of the oscillator output signal feeds back to the circulator as the self-injection signal. In the feedback loop, the delay cable, high- Q factor resonator, or amplifier, may be used. The phase noise is reduced after self-injection locking as compared to the phase noise of the free-running oscillator while satisfying the stability conditions.

In this paper, a proposed feedback topology is presented. Part of the oscillator output power injects to the current source directly rather than going through the circulator and returning to the oscillator output port. Under the stable oscillation conditions, the feedback push–push signal ($2f_o$) can be transformed to a stable signal with larger amplitude to improve the oscillator phase noise. The larger signal injection can be achieved because of the larger transconductance (g_{m1}) of the current source rather than the small-signal injection in the reported literatures [19]–[21]. The phase noise of the push–push oscillator using the proposed feedback topology shown in Fig. 1(b), without a circulator and an external amplifier, rivals the phase noise of the push–push oscillator using the regular feedback topology with a circulator shown in Fig. 1(a). The analysis procedures in this paper are based on the methods proposed in [20]–[27]. However, it is the first attempt to analyze the amplitude and phase stability, as well as phase-noise reduction for the proposed second-harmonic self-injected push–push oscillator.

This paper is organized as follows. In Section II, the second-harmonic self-injected oscillator topology is presented,

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The authors are with the Department of Electrical Engineering and the Graduate Institute of Communication Engineering, National Taiwan University, Taipei, Taiwan 10617, R.O.C. (e-mail: huei.wang@ew.ee.ntu.edu.tw).

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Fig. 1. Setups for: (a) the regular self-injection-locked oscillator and (b) the proposed self-injected push-push oscillator.

the stability conditions of amplitude fluctuation and phase fluctuation of the fundamental signal (f_o) and push-push signal ($2f_o$) are analyzed, and the phenomena of the phase-noise reductions for the push-push signal ($2f_o$) are also derived in detail. Section III gives the circuit design method and device-size selections. Section IV gives experimental results and characterization. Section V gives the conclusions.

II. STABILITY CONDITIONS AND PHASE-NOISE ANALYSIS OF THE PROPOSED CIRCUIT TOPOLOGY

A. Amplitude Stability Analysis

The circuit topology of the second-harmonic self-injected push-push oscillator is shown in Fig. 2. The oscillator consists of a cross-coupled pair (M_2 – M_3), a current source (M_1), a power splitter, and a tunable delay path containing a delay-line cable and a tunable phase shifter. The fundamental frequency (ω_o) of the oscillator is $1/\sqrt{LC}$. In order to analyze the behavior of the second-harmonic self-injected oscillator easily, Fig. 3 shows the simplified oscillator model consisting of an LC tank, a conductance (G_t) representing the tank loss, a feedback signal ($V_f(t)$), and the mildly nonlinear transconductances (g_{m1} to g_{m3}). An oscillator's noise can be modeled by a noise-current source or a complex noise admittance ($Y_n = G_n + jB_n$) [24] shown in Fig. 3. G_n physically represents the oscillator amplitude fluctuations and B_n physically represents the oscillator phase fluctuations. This complex noise admittance (Y_n) is used for the phase-noise reduction analysis.

For the amplitude and phase stability analysis, the dynamic equation for this oscillator shown in Fig. 3 is derived as

$$C \frac{d^2(V_R - V_L)}{dt^2} + G_t \frac{d(V_R - V_L)}{dt} + \frac{1}{L}(V_R - V_L) = g_{m2} \frac{dV_R}{dt} - g_{m1} \frac{dV_f}{dt}. \quad (1)$$

Fig. 2. Circuit topology of the self-injected push-push oscillator.

Fig. 3. Simplified push-push oscillator model.

The free-running voltages (V_L and V_R) with harmonic terms are assumed time variant and are written as

$$\begin{aligned} V_R(t) &= (A_o(t) + \Delta A_o(t))e^{j(\omega_o t + \theta_o(t))} \\ &\quad + (A_1(t) + \Delta A_1(t))e^{j(2\omega_o t + \theta_1(t))} + \dots \\ V_L(t) &= -A_o(t)e^{j(\omega_o t + \theta_o(t))} + A_1(t)e^{j(2\omega_o t + \theta_1(t))} + \dots \end{aligned} \quad (2)$$

(3)

where $A_o(t)$ and $A_1(t)$ are the fundamental and second harmonic amplitudes of oscillation, respectively. $\Delta A_o(t)$ is the amplitude mismatch of the fundamental signals for $V_R(t)$ and $V_L(t)$. $\Delta A_1(t)$ is the amplitude mismatch of the second harmonic signals for $V_R(t)$ and $V_L(t)$. The $(\omega_o + \theta_o(t))$ and $(2\omega_o + \theta_1(t))$ are the instantaneous phases of fundamental and second harmonic amplitudes of oscillation, respectively.

For the self-injected push–push oscillator, part of the output signal feeds back to the current source. The current source with the mildly nonlinear transconductance (g_{m1}) transforms the feedback signal ($V_f(t)$) to a larger current format ($I_f(t) = g_{m1} \cdot V_f(t)$). With the equivalent parallel resistance of the tank (R_{eq}) for the second harmonic ($2f_o$), the feedback-signal amplitude crossing the tank (V_{inj}) is produced ($V_{inj}(t) = I_f(t) \cdot R_{eq}$). This tank amplitude may be larger than the second harmonic amplitude ($|A_1|$) generated by the cross-coupled pair (M_2 – M_3) if the path loss in the feedback loop is small. This situation is $|V_{inj}| \geq |A_1|$ rather than the low-power injection ($|V_{inj}| < |A_1|$) in [20] and [21]. The dynamic amplitude behaviors are not considered in [20] and [21] due to the low-power injection. However, the dynamic amplitude behaviors of this study are needed to be considered because of the large-signal injection (V_{inj}).

For the push–push oscillator in Fig. 3, the differential fundamental signals are almost canceled in the feedback path. Only the second harmonic signal without amplitude mismatch is considered in the feedback path. Other high-order harmonic signals are also neglected due to the relative small amplitudes of oscillations. Therefore, the feedback signal can be written as

$$V_f(t) = \frac{2A_1(t)}{K} e^{j(2\omega_o t + \theta_f)} \quad (4)$$

where K is the amplitude-attenuation factor of the delay path and θ_f is the constant phase parameter. Substitute (2)–(4) into (1) and separate the real and imaginary parts of the fundamental signal (f_o) and second harmonic signal ($2f_o$), respectively. The real and imaginary parts of the dynamic equations for fundamental signal (f_o) can be written as

$$C \frac{d^2(2A_o)}{dt^2} + G_t \frac{d(2A_o)}{dt} + \left(\frac{1}{L} - C \left(\omega_o + \frac{d\theta_o}{dt} \right)^2 \right) (2A_o) = g_{m2} \frac{dA_o}{dt}. \quad (5)$$

$$2C \left(\omega_o + \frac{d\theta_o}{dt} \right) \frac{d(2A_o)}{dt} + 2A_o \frac{d^2\theta_o}{dt^2} + G_t(2A_o) \left(\omega_o + \frac{d\theta_o}{dt} \right) = g_{m2} A_o \left(\omega_o + \frac{d\theta_o}{dt} \right). \quad (6)$$

The real and imaginary parts of the dynamic equations for the second harmonic signal ($2f_o$) can be derived as

$$C \frac{d^2(\Delta A_1)}{dt^2} - C(\Delta A_1) \left(2\omega_o + \frac{d\theta_1}{dt} \right)^2 + G_t \frac{d(\Delta A_1)}{dt} + \frac{\Delta A_1}{L} = g_{m2} \frac{dA_1}{dt} - \frac{2g_{m1}}{K} \left(\frac{dA_1}{dt} \right) \cos(\theta_f - \theta_1(t)) + \frac{2g_{m1}}{K} A_1 \cdot (2\omega_o) \sin(\theta_f - \theta_1(t)) \quad (7)$$

$$2C \left(2\omega_o + \frac{d\theta_1}{dt} \right) \frac{d(\Delta A_1)}{dt} + G_t(\Delta A_1) \frac{d^2\theta_1}{dt^2} + G_t(\Delta A_1) \left(2\omega_o + \frac{d\theta_1}{dt} \right) = g_{m2} A_1 \left(2\omega_o + \frac{d\theta_1}{dt} \right) - \frac{2g_{m1}}{K} \left(\frac{dA_1}{dt} \right) \sin(\theta_f - \theta_1(t)) - \frac{2g_{m1}}{K} A_1 \cdot (2\omega_o) \cos(\theta_f - \theta_1(t)). \quad (8)$$

In order to simplify these equations, the amplitude, phase, and phase derivatives are assumed to vary slowly in (5) and (7). Phase is also assumed to vary slowly in (6) and (8). Therefore, the amplitude and phase dynamic equations (5)–(8) become

$$\frac{d\theta_o}{dt} = 0 \quad (9)$$

$$\frac{dA_o}{dt} = -\frac{2G_t - g_{m2}}{4C} A_o \quad (10)$$

$$\frac{d\theta_1}{dt} = \frac{-3}{8} \cdot (2\omega_o) - \frac{g_{m1} R_L \cdot (2\omega_o)}{2KQ} \frac{A_1}{\Delta A_1} \sin(\theta_f - \theta_1(t)) \quad (11)$$

$$\frac{dA_1}{dt} = \frac{g_{m2} A_1 (2\omega_o) - G_t(\Delta A_1) \cdot (2\omega_o)}{\frac{2g_{m1}}{K} \sin(\theta_f - \theta_1(t))} - \frac{\frac{2g_{m1}}{K} A_1 (2\omega_o) \cos(\theta_f - \theta_1(t))}{\frac{2g_{m1}}{K} \sin(\theta_f - \theta_1(t))}. \quad (12)$$

The Q in (11) is the quality factor defined as $Q = R_L/\omega_o L$ of the LC tank. R_L is the equivalent parallel resistance of the tank for the fundamental signal (f_o). For the amplitude stability analysis, perturbations are characterized as $A_o \rightarrow \hat{A}_o + \delta A_o$, $A_1 \rightarrow \hat{A}_1 + \delta A_1$ and $\theta_1 \rightarrow \hat{\theta}_1 + \delta \theta_1$, where $\hat{A}_o$ and $(\hat{A}_1, \hat{\theta}_1)$ are the steady-state solutions for (10) and (12), respectively. δA_o , δA_1 , and $\delta \theta_1$ are also the amplitude and phase fluctuations of the oscillator, respectively. If these fluctuations are small, (10) and (12) can be linearized around $\hat{A}_o$ and $(\hat{A}_1, \hat{\theta}_1)$, respectively, and become

$$\frac{d\delta A_o}{dt} = -\delta A_o \frac{2G_t - g_{m2}}{4C} \quad (13)$$

$$\begin{aligned} \frac{d\delta A_1}{dt} = & -\delta A_1 (2\omega_o) \\ & \times \frac{-g_{m2} + \frac{2g_{m1}}{K} \cos(\theta_f - \hat{\theta}_1) + G_t \frac{\Delta(\delta A_1)}{\delta A_1}}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)} \\ & - (2\omega_o) \frac{\frac{2g_{m1}}{K} \hat{A}_1 \sin(\theta_f - \hat{\theta}_1)(\delta \theta_1)}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)}. \end{aligned} \quad (14)$$

For the stable amplitude, the amplitude fluctuations (13)–(14) for fundamental signal (f_o) and second harmonic signal ($2f_o$) need to approach zero, respectively. The stable condition for (13) is $2G_t > g_{m2}(R_t/2 < 1/g_{m2})$, which means the tank loss ($R_t/2$) is smaller than $1/g_{m2}$. In order to let (14) approach zero, $\delta \theta_1$ is zero by assuming that the second harmonic frequency is stable. Equation (14) can then be simplified as

$$\frac{d\delta A_1}{dt} = -\delta A_1 (2\omega_o) \frac{-g_{m2} + \frac{2g_{m1}}{K} \cos(\theta_f - \hat{\theta}_1) + G_t \frac{\Delta(\delta A_1)}{\delta A_1}}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)}. \quad (15)$$

$\Delta(\delta A_1)$ is similar to δA_1 in (15). In order to let (15) approach zero, the denominator and numerator need to be simultaneously greater than zero or smaller than zero. The conditions approximate $2G_t > g_{m2}$ and

$$2n\pi < \theta_f - \hat{\theta}_1 < (2n+1)\frac{\pi}{2} \quad (16)$$

where $\theta_f - \hat{\theta}_1$ is the phase delay shown in Fig. 2, and n is an integer.

B. Phase-Stability Analysis

For the phase-stability analysis, (9) and (11) are used to analyze the phase stability of the fundamental signal (f_o) and second harmonic signal ($2f_o$) for the self-injected push-push oscillator, respectively. Perturbations are characterized as $\theta_o \rightarrow \hat{\theta}_O + \delta\theta_o$ and $\theta_1 \rightarrow \hat{\theta}_1 + \delta\theta_1$, where $(\hat{\theta}_O, \hat{\theta}_1)$ are the steady-state solutions and $(\delta\theta_o, \delta\theta_1)$ are the phase fluctuations. Equations (9) and (11) can then be written as

$$\begin{aligned} \frac{d(\delta\theta_o)}{dt} &= 0 \\ \frac{d(\hat{\theta}_1 + \delta\theta_1)}{dt} &= \frac{-3}{8} \cdot (2\omega_o) \\ &\quad - \frac{g_{m1}R_L \cdot (2\omega_o)}{2KQ} \frac{\hat{A}_1}{\Delta A_1} \cos(\theta_f - \hat{\theta}_1) \cdot \delta\theta_1 \\ &\quad - \frac{g_{m1}R_L \cdot (2\omega_o)}{2KQ} \frac{\delta A_1}{\Delta A_1} \sin(\theta_f - \hat{\theta}_1). \end{aligned} \quad (17)$$

From (17), the phase fluctuation of the fundamental signal (f_o) equals zero. Therefore, fundamental frequency will be phase stable at f_o . In (18), assuming the phase fluctuations are small, and δA_1 is zero due to amplitude stable, then (18) can be linearized around $\hat{\theta}_1$, and it becomes

$$\frac{d\delta\theta_1}{dt} = -\frac{g_{m1}R_L \cdot (2\omega_o)}{2KQ} \frac{\hat{A}_1}{\Delta A_1} \cos(\theta_f - \hat{\theta}_1) \cdot \delta\theta_1. \quad (19)$$

In order to stabilize the phase, the phase fluctuation (19) needs to approach zero. The condition is

$$\cos(\theta_f - \hat{\theta}_1) > 0, \quad (-(2n+1)\pi/2 < \theta_f - \hat{\theta}_1 < (2n+1)\pi/2). \quad (20)$$

where $\theta_f - \hat{\theta}_1$ is the feedback phase delay shown in Fig. 2, and n is an integer. From (19), with a larger transconductance (g_{m1}) of current source, a larger equivalent parallel resistance of the tank (R_L) for the fundamental signal (f_o), a lower amplitude-attenuation factor (K) of the delay path, smaller amplitude imbalance (ΔA_1) for the second harmonic signal, and higher second harmonic amplitude ($\hat{A}_1$), the phase fluctuation of the second harmonic signal ($2f_o$) decreases with time more quickly. Therefore, the oscillator will be phase stable.

C. Phase-Noise Reduction of the Self-Injected Push-Push Oscillator

For the phase-noise reduction analysis of the push-push signal ($2f_o$), the dynamic equations for the amplitude and phase of the self-injected push-push oscillator including the complex noise admittance ($Y_n = G_n + jB_n$), shown in Fig. 3, are (21) and (22), shown at the bottom of this page.

$G_{n1}(t)$ and $B_{n1}(t)$ in (21) and (22) physically represent the amplitude fluctuation and phase fluctuation of the second harmonic signal ($2f_o$), respectively. Assume (21) and (22) are perturbed by $A_1 \rightarrow \hat{A}_1 + \delta A_1$ and $\theta_1 \rightarrow \hat{\theta}_1 + \delta\theta_1$, where $(\hat{A}_1, \hat{\theta}_1)$ are the steady-state solutions for (21) and (22), and $(\delta A_1, \delta\theta_1)$ are the amplitude and phase fluctuations of the second harmonic signal ($2f_o$) for the oscillator, respectively. If these fluctuations are small, (21) and (22) can be linearized around $(\hat{A}_1, \hat{\theta}_1)$ and become (23) and (24), shown at the bottom of this page. The spectral characteristic of the amplitude and phase fluctuations can be obtained by Fourier transforming (23) and (24). Equations (23) and (24) then become (25) and (26), shown at the bottom of the following page.

The tilde ($\sim$) presents the variables in the transformed or spectral domain, and ω is the noise frequency measured relative to the carrier. In (25), the first term on the right-hand side represents the AM-to-AM noise, and the second term represents the conversion of PM noise to AM noise. In (26), the first term on the right-hand side represents the PM-to-PM noise, and the

$$\begin{aligned} \frac{dA_1}{dt} &= \frac{g_{m2}[(A_1 + \Delta A_1)\omega_o] - \frac{2g_{m1}}{K} A_1(2\omega_o) \cos(\theta_f - \theta_1(t))}{\frac{2g_{m1}}{K} \sin(\theta_f - \theta_1(t)) + 2B_{n1}(t)} \\ &\quad - \frac{2c(2\omega_o) \frac{d(\Delta A_1)}{dt} + (G_t + G_{n1}(t))(\Delta A_1)(2\omega_o) + B_{n1}(t) \frac{d(\Delta A_1)}{dt}}{\frac{2g_{m1}}{K} \sin(\theta_f - \theta_1(t)) + 2B_{n1}(t)} \end{aligned} \quad (21)$$

$$\frac{d\theta_1}{dt} = -\frac{3 + (2\omega_o)LB_{n1}(t) + \frac{2g_{m1}L}{K}(2\omega_o) \sin(\theta_f - \theta_1(t)) \frac{A_1}{\Delta A_1}}{\frac{4}{\omega_o} + LB_{n1}(t)} \quad (22)$$

$$\frac{d\delta A_1}{dt} = \frac{\delta A_1 \left(g_{m2}\omega_o - \frac{2g_{m1}}{K}(2\omega_o) \cos(\theta_f - \hat{\theta}_1) \right)}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)} + \frac{\delta\theta_1 \cdot \hat{A}_1 \frac{2g_{m1}}{K}(2\omega_o) \sin(\theta_f - \hat{\theta}_1)}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)} - \frac{\delta A(G_t + G_{n1}(t))(2\omega_o)}{\frac{2g_{m1}}{K} \sin(\theta_f - \hat{\theta}_1)} \quad (23)$$

$$\frac{d\delta\theta_1}{dt} = \frac{-(2\omega_o)LB_{n1}(t) + \delta\theta_1(t) \cdot \frac{2g_{m1}L}{K}(2\omega_o) \cos(\theta_f - \theta_1(t)) \frac{\hat{A}_1}{\Delta A_1}}{\frac{4}{\omega_o} + LB_{n1}(t)} - \frac{\frac{2g_{m1}L}{K}(2\omega_o) \sin(\theta_f - \theta_1(t)) \frac{\delta A_1}{\Delta A_1}}{\frac{4}{\omega_o} + LB_{n1}(t)} \quad (24)$$

second term on the right-hand side represents the conversion of AM-to-PM noise. For a practical oscillator, the amplitude fluctuation is significantly attenuated by the amplitude limiting mechanism. Therefore, the AM-to-PM noise conversion is negligible in the phase-noise analysis and focus here will be on PM-to-PM noise. As a result, the phase fluctuations (26) of the push-push oscillator can be arranged as

$$\widetilde{\delta\theta_1}(\omega) = \frac{\widetilde{B_{n1}}(\omega)}{\frac{\widehat{A_1}}{\Delta A_1} \frac{2g_{m1}}{K} \cos(\theta_f - \widehat{\theta_1}) - j \frac{\omega}{\omega_{3\text{ dB}} R_L}} \quad (27)$$

where $\omega_{3\text{ dB}} = \omega_o/2Q$, half the 3-dB bandwidth of the oscillator tank circuits. The power spectrum of the self-injected push-push oscillator's fluctuations is given by $\langle \widetilde{\delta\theta_1} \widetilde{\delta\theta_1}^* \rangle$, where the notation $\langle \rangle$ represents an ensemble average. The power spectral density of the oscillator's phase fluctuation (i.e., phase noise) is then

$$|\widetilde{\delta\theta_1}(\omega)|^2 = \frac{|\widetilde{B_{n1}}(\omega)|^2}{\left(\frac{\widehat{A_1}}{\Delta A_1} \frac{2g_{m1}}{K} \cos(\theta_f - \widehat{\theta_1}) \right)^2 + \left(\frac{\omega}{\omega_{3\text{ dB}} R_L} \right)^2}. \quad (28)$$

When the oscillator is in the free-running state without self-injection feedback current ($I_f = g_{m1} \cdot V_f$). The transconductance (g_{m1}) can be assumed zero in (28) because the g_{m1} in (28) deals with the feedback signal shown in Fig. 3. The free-running phase noise can be written as

$$|\widetilde{\delta\theta_1}(\omega)|_{\text{free}}^2 = \frac{|\widetilde{B_{n1}}(\omega)|^2}{\left(\frac{\omega}{\omega_{3\text{ dB}} R_L} \right)^2}. \quad (29)$$

Substituting (29) into (28), the phase fluctuation (i.e., phase noise) of the oscillator becomes

$$|\widetilde{\delta\theta_1}(\omega)|^2 = \frac{|\widetilde{\delta\theta_1}(\omega)|_{\text{free}}^2}{\left(\frac{\widehat{A_1}}{\Delta A_1} \frac{2g_{m1}}{K} \cos(\theta_f - \widehat{\theta_1}) \cdot \frac{\omega_{3\text{ dB}} R_L}{\omega} \right)^2 + 1}. \quad (30)$$

The different phase delays ($\theta_f - \widehat{\theta_1}$) in (30) are considered separately as follows.

1) *Phase-Delay Loop ($\theta_f - \widehat{\theta_1}$) Approximate to $2n\pi$* : While the oscillator is in the self-injection state with the phase-delay loop, ($\theta_f - \widehat{\theta_1}$), shown in Fig. 2, approximates to $2n\pi$, where n is an integer. From (16) and (20), the oscillator is stable. From (30), the power spectral density of the oscillator's phase fluctuation

(i.e., phase noise) becomes

$$|\widetilde{\delta\theta_1}(\omega)|^2 = \frac{|\widetilde{\delta\theta_1}(\omega)|_{\text{free}}^2}{\left(\frac{\widehat{A_1}}{\Delta A_1} \frac{2g_{m1}}{K} \cdot \frac{\omega_{3\text{ dB}} R_L}{\omega} \right)^2 + 1} \quad (31)$$

which can be reduced further by increasing the transconductance (g_{m1}) of the current source, increasing the equivalent parallel-resistance of the tank (R_L) for the fundamental signal (f_o), reducing the amplitude-attenuation factor (K) of the delay path, reducing amplitude imbalance (ΔA_1) for second harmonic signal, and increasing second harmonic amplitude ($\widehat{A_1}$). From (31), the closer to the carrier frequency, the lower the phase noise can be obtained. However, the phase-noise improvement will be limited if the free-running oscillator already has good phase noise. This is because a low phase-noise oscillator typically has a small half the 3-dB bandwidth of the oscillator tank circuits ($\omega_{3\text{ dB}} = \omega_o/2Q$) or a high quality factor (Q) of the LC tank. From (31), at the frequencies far from the carrier, the phase noise reduces to that of free-running oscillator noise properties

$$\lim_{\omega \rightarrow \infty} |\widetilde{\delta\theta_1}(\omega)|^2 = |\widetilde{\delta\theta_1}(\omega)|_{\text{free}}^2. \quad (32)$$

2) *Phase-Delay Loop ($\theta_f - \widehat{\theta_1}$) Approximate to $(2n+1)\pi$* : When the oscillator is in the self-injection state with the phase-delay loop ($\theta_f - \widehat{\theta_1}$), the value of the phase-delay loop is set at approximately $(2n+1)\pi$, where n is an integer. From (15), (16), (19), and (20), the amplitude and phase fluctuations increase with time, and the amplitude and phase difference are unstable. The phase noise becomes worse than that in the free-running state.

D. $1/f$ Noise Upconversion in Second-Harmonic Self-Injected Push-Push Oscillator

The Hajimiri's time-varying phase-noise theory [26] is also adopted to analyze the second-harmonic self-injected push-push oscillator. The impulse sensitivity function (ISF) is dimensionless with period 2π , which describes how much phase shift results from applying a unit impulse. Since ISF is a periodic function with period 2π , it can be written in a Fourier series

$$\Gamma(\omega_o\tau) = \frac{c_o}{2} + \sum_{n=1}^{\infty} c_n \cos(n\omega_o\tau + \theta_n) \quad (33)$$

where the c_n terms are the real-value coefficients, and θ_n is the phase of the n th harmonic. With the Fourier coefficients in (33),

$$j\omega \widetilde{\delta A_1} = - \frac{\delta \widehat{A_1} \left(\frac{2g_{m1}}{K} (2\omega_o) \cos(\theta_f - \widehat{\theta_1}) + (2\omega_o)(G_t + \widetilde{G_{n1}}(\omega)) - g_{m2}\omega_o \right)}{\frac{2g_{m1}}{K} \sin(\theta_f - \widehat{\theta_1})} + \frac{\widetilde{\delta\theta_1} \cdot \widehat{A_1} \frac{2g_{m1}}{K} (2\omega_o) \sin(\theta_f - \widehat{\theta_1})}{\frac{2g_{m1}}{K} \sin(\theta_f - \widehat{\theta_1})} \quad (25)$$

$$j\omega \widetilde{\delta\theta_1} = \frac{(\widetilde{\delta\theta_1}) \frac{\widehat{A_1}}{\Delta A_1} \frac{2g_{m1}L}{K} (2\omega_o) \cos(\theta_f - \widehat{\theta_1}) - (2\omega_o)L\widetilde{B_{n1}}(\omega)}{\frac{4}{\omega_o} + L\widetilde{B_{n1}}(\omega)} - \frac{\frac{2g_{m1}L}{K} \frac{\delta \widehat{A_1}}{\Delta(\delta A_1)} (2\omega_o) \sin(\theta_f - \widehat{\theta_1})}{\frac{4}{\omega_o} + L\widetilde{B_{n1}}(\omega)} \quad (26)$$

Fig. 4. ISFs of push–push signals ($2f_o$) for the free-running push–push oscillator without feedback and the stable self-injected push–push oscillator with 45° phase delay ($\theta_f - \hat{\theta}_1$).

the relationship of the device noise $1/f$ corner frequency and the $1/f^3$ corner in the phase spectrum can be written as [26]

$$\omega_{1/f^3} = \omega_{1/f} \cdot \frac{c_o^2}{2\Gamma_{\text{rms}}^2} \quad (34)$$

where c_o is the twice of the dc value of the ISF and Γ_{rms} is the root mean square value of the ISF. From (34), the $1/f$ noise up-conversion can be significantly reduced by minimizing c_o . Since c_o is twice the dc value of the ISF over a period, reduction of the phase noise in the $1/f^3$ region can be achieved by minimizing the dc value of the ISF [26], [27].

In order to obtain the dc values of the ISFs, the ISFs are calculated using the approximate analytical method in [26]. Although this method is an approximation, it is the easiest to use and rapidly develops important insights into the behavior of an oscillator [26], [27]. Fig. 4 shows the calculated ISFs of the push–push signals ($2f_o$) for the free-running push–push oscillator without feedback and the stable second-harmonic self-injected push–push oscillator with 45° phase delay ($\theta_f - \hat{\theta}_1$). The absolute dc values for the ISFs of the free-running push–push oscillator without feedback and the stable second-harmonic self-injected push–push oscillator with 45° phase delay ($\theta_f - \hat{\theta}_1$) are calculated as 0.0031 and 0.002, respectively. The absolute ISF dc value of the free-running push–push oscillator is 1.55 times larger than the other one. This means that the free-running push–push oscillator has a larger $1/f$ noise upconversion factor, leading to a worse phase noise in the $1/f^3$ region. From time-varying phase-noise theory [26], the square of the dc value of the ISF is proportional to the phase noise in the $1/f^3$ region. Therefore, from the ISF calculation, the phase noise in the $1/f^3$ region of the free-running push–push oscillator is approximately 3.8 dB worse than the self-injected push–push oscillator with 45° phase delay.

III. CIRCUIT DESIGN

A. Oscillator Topology and Phase-Delay Loop Consideration

The push–push oscillator core was implemented in a commercial $0.18\text{-}\mu\text{m}$ bulk CMOS technology. The circuit

schematic of the X-band self-injected push–push oscillator has been shown in Fig. 2. The oscillator core is composed of an LC tank and a cross-coupled pair with each nMOS of 32 fingers and total gatewidth of $80\text{ }\mu\text{m}$. The larger CMOS devices with lower flicker noise were used in the oscillator design. The total gatewidth of the current source (M_1) is $160\text{ }\mu\text{m}$.

The negative- g_m initiates oscillation at the fundamental frequency (f_o) across the output of the cross-coupled pair along with the harmonic components. The output node is located in the middle of the inductor, behaving as a virtual ground for the differential mode and an open circuit for the common mode with respect to the cross-coupled pair. The out-of-phase fundamental components are cancelled, while the in-phase harmonic components sum up at this node. As a result, an enhanced component at the frequency twice of the LC resonant frequency appears as the oscillator output.

For the self-injected push–push oscillator, a part of the output signal is extracted from the power splitter, then passing through the tunable delay-line path and returning to the gate of the current source. For a stable oscillator, the amplitude fluctuations (15) and phase fluctuations (19) need to approach zero. The amplitude- and phase-stability conditions (16) and (20) have to be satisfied. From (16) and (20), the phase delay shown in Fig. 2 has to be in the range

$$2n\pi < \theta_f - \hat{\theta}_1 < (2n+1)\frac{\pi}{2} \quad (35)$$

where n is an integer. From (30), the phase noise can be further reduced near the carrier frequency by using the high-transconductance (g_{m1}) current source with $160\text{-}\mu\text{m}$ gatewidth, and using the low-loss delay path with low amplitude-attenuation factor (K). A push–push oscillator using a regular self-injection delay path was also designed for comparison.

B. MOS Device Size Consideration

In the oscillator design, the device size has to be considered. The active devices have influences on the oscillator performances such as phase noise, power consumption, oscillating frequency, and the figure-of-merit. In CMOS design, the MOSFET flicker noise ($1/f$ noise) at low frequencies generally exhibits a spectral density of the input referred voltage noise ($\overline{V_n^2}$) described in [28, p. 343]

$$\overline{V_n^2} = \frac{M}{C_{\text{ox}}W_gL_g} \cdot \frac{1}{f} \quad (36)$$

where M is the process-dependent constant, C_{ox} is the oxide capacitance, W_g is the gatewidth, and L_g is the gate length. The voltage noise is inversely proportional to the frequency f , and the MOS gate area ($W_g \cdot L_g$). Increasing the gate area ($W_g \cdot L_g$) with constant W_g/L_g and fixed bias results in lower $1/f$ noise. However, this will trade off with power consumption and the $1/f$ noise. In order to reduce the noise contribution to the self-injected push–push oscillator, the $160\text{-}\mu\text{m}$ gatewidth nMOS serves as the current source for lower flicker noise ($1/f$ noise) consideration.

For the cross-coupled pair in the oscillator, the simulated performance with different $0.18\text{-}\mu\text{m}$ nMOS gate area ($W_g \cdot L_g$) and different bias conditions are shown in Table I. From this

TABLE I
SIMULATED PERFORMANCE OF THE FREE-RUNNING CROSS-COUPLED OSCILLATORS WITH DIFFERENT DEVICE SIZES AND BIAS CONDITIONS

Device of Cross-Coupled Pair (W_g (μm) / L_g (μm))	Device of Current Source (W_g (μm) / L_g (μm))	V_{DD} (V)	Power Consumption (mW)	Oscillating Frequency (GHz)	Output Power (dBm)	Phase Noise at 1 MHz (dBc/Hz)	Figure of Merit (dBc/Hz)
40/0.18	160/0.18	1.5	27	10.3	-2.6	-117.9	-180.1
60/0.18	160/0.18	1.5	28.3	9.9	-1.4	-116.8	-182.2
80/0.18	160/0.18	1.5	28.8	9.6	-1.2	-117.5	-182.6
40/0.18	160/0.18	1.0	9.9	10.4	-10.5	-113.5	-183.8
60/0.18	160/0.18	1.0	12.3	10	-7.6	-115	-184
80/0.18	160/0.18	1.0	13.9	9.6	-6.2	-116.4	-184.6

table, using a larger gate-area device in the oscillator cross-coupled pair, lower oscillator phase noise, better figure-of-merit, and higher output power can be obtained under the same bias conditions and the same device-size current sources. However, using a larger gate-area device will consume a little more dc power.

Typically, an oscillator operating at low frequency has better phase noise than that of an oscillator operating at high frequency. A low phase-noise oscillator can be achieved by increasing the power consumption. Therefore, there is a tradeoff between oscillator phase noise and power consumption. In order to evaluate the performance of an oscillator, the figure-of-merit considering the phase noise, carrier frequency, and power consumption is widely adopted in the oscillator papers, e.g., the figure-of-merit is used in [29]–[31], [33], and [39]. The performance of an oscillator evaluated by the figure-of-merit including the phase noise $L(f_{\text{offset}})$, carrier frequency (f_o), offset frequency (f_{offset}), and dc power consumption (P_{DC}) can be defined by

$$L(f_{\text{offset}}) - 20 \log \left(\frac{f_o}{f_{\text{offset}}} \right) + 10 \log \left(\frac{P_{DC}}{1 \text{ mW}} \right). \quad (37)$$

The first and third terms of (37) represent the contributions of phase noise and power consumption to figure-of-merit, respectively. In (37), the values of the figure-of-merit and phase noise are denoted with a negative sign, and the power consumption is denoted with a positive sign. Therefore, the figure-of-merit is linearly proportional to the phase noise, and the figure-of-merit is inversely proportional to the $10 \log(P_{DC}/1\text{mW})$. The phase noise has greater and more direct impact on figure-of-merit than the power consumption (P_{DC}) does for a fixed operating frequency (f_o). As a result, from (37) and Table I, using larger gate-area devices in the cross-coupled pair turns out to be a better design approach in this study. Fig. 5 shows the simulated phase noise of the free-running state, unstable state of self-injection, and stable state of self-injection for the push–push signal ($2f_o$) of the oscillator with a total 160- μm gatewidth current source and a cross-coupled pair with each total 80- μm gatewidth nMOS device. The phase noise of the free-running push–push oscillator is improved by using the proposed self-injection feedback loop under stability conditions.

Fig. 5. Simulated phase noise of the free running state, unstable state of self-injection, and stable state of self-injection for the push–push signal ($2f_o$) of this oscillator.

C. Inductor Consideration

The oscillator uses on-chip inductors in the LC tank, and an external RF choke shown in Fig. 2 is used to isolate supply voltage (V_{DD}) from the feedback path for the push–push signal ($2f_o$) for the flexibility consideration. The push–push signal ($2f_o$) generated from the cross-coupled pair will go to the oscillator output port where it is almost not affected by the supply voltage (V_{DD}) because of the high-impedance RF choke.

For a single-chip self-injected push–push oscillator in the future, from [4] and [5], in order to obtain a high impedance looking toward the bias (V_{DD}) for the second harmonic signal ($2f_o$), the bias circuits of the push–push oscillator consist of an RF bypass capacitor and a $\lambda/4$ coplanar waveguide (CPW) for the push–push signal ($2f_o$). For an X -band push–push oscillator design shown in Fig. 2, the bias circuit can be implemented with a 4-pF on-chip bypass capacitor and a 5-nH on-chip miniature 3-D inductor [37]. For the 5-nH on-chip inductor, the measured Q factor is 6.2 at 10 GHz, and the self-resonance frequency is 16 GHz [37].

Table II gives the simulated free-running oscillator phase-noise data at 1-MHz offset with respect to different Q factors of a 5-nH on-chip RF-choke inductor. From this table, the phase noise degrades only 0.43 dB (from -116.17

TABLE II
SIMULATED FREE-RUNNING OSCILLATOR PHASE NOISE WITH RESPECT
TO Q -FACTORS OF THE 5-nH ON-CHIP RF-CHOKE INDUCTOR

Q -Factor	Oscillator Phase Noise at 1-MHz Offset (dBc/Hz)
4	-115.74
6	-116.06
8	-116.11
10	-116.14
12	-116.16
14	-116.17

to -115.74 dBc/Hz) when the Q factor reduces by 10 (from 14 to 4). In addition, the oscillator phase noise with respect to different Q factors of the 0.7-nH on-chip inductor of the LC tank used in this design is also investigated. The simulated free-running oscillator phase noise degrades 6.7 dB (from -117.9 to -111.2 dBc/Hz) when the Q factors of the 0.7-nH inductor reduce by 10 (from 14 to 4).

As a result, the phase noise of the self-injected push-push oscillator is dominated by the Q factor of the 0.7-nH on-chip inductor of the LC tank. The simulated Q factor of the 0.7-nH on-chip inductor is 14.5 at 10 GHz in this design. For an oscillator with on-chip RF choke in the future, the simulated phase noise of the free-running push-push oscillator with fully integrated on-chip RF choke approximates -116 dBc/Hz at 1-MHz offset, and this value is similar to that of the free-running push-push oscillator with external RF choke in this design.

IV. MEASURED RESULTS OF THE SELF-INJECTED PUSH-PUSH OSCILLATORS

Fig. 6 shows the photograph of the fabricated $0.18\text{-}\mu\text{m}$ push-push CMOS oscillator with a chip size of $0.61\text{ mm} \times 0.63\text{ mm}$ including the testing pads. On-wafer probing was performed to characterize the performance of the oscillator. The phase-noise characteristic of the oscillator is measured using the Agilent E4448A spectrum analyzer. The free-running phase noise can be measured directly from the oscillator output without a power splitter and a feedback path or from one of the power splitter's output ports while the other splitter's output port is connected with the $50\text{-}\Omega$ load. The measured free-running phase noise is similar for these two cases. The free-running phase noise is -116.1 dBc/Hz at 1-MHz offset from the carrier, as shown in Fig. 7. The oscillator supply voltage (V_{DD}) is 1.0 V, and the dc power consumption is 13.8 mW. The oscillator is self-injected by a part of its output power through the off-chip power splitter, delay-line cable, and tunable phase shifter with the total phase delay ($\theta_f - \theta_1$) shown in Fig. 2 approximating 45° . From (35), the oscillator is in the stable range. The measured output power is -14 dBm at 9.6-GHz oscillating frequency after calibrating the path loss, and the fundamental rejection is 45 dB.

Fig. 8 shows the measured phase noise from 100 kHz to 10 MHz of the push-push signals ($2f_o$) for the free-running push-push oscillator and the stable second-harmonic self-injected push-push oscillator with 45° phase delay ($\theta_f - \theta_1$).

Fig. 6. Chip photograph with the chip size $0.61\text{ mm} \times 0.63\text{ mm}$ of the push-push oscillator.

Fig. 7. Measured phase noise of the free-running push-push oscillator at a 9.6-GHz output frequency. (-116.1 dBc/Hz at 1-MHz offset from the carrier. The resolution bandwidth is 91 kHz.)

From this figure, the $1/f^3$ phase-noise corner frequency is formed at the offset frequency around 1.1 MHz in the self-injected push-push oscillator. The measured phase noise of the self-injected push-push oscillator with 45° phase delay is improved approximately 4 dB at 1-MHz offset from the free-running push-push oscillator. The dotted line represents the calculated phase noise in the $1/f^3$ portion for the self-injected push-push oscillator with 45° phase delay. The calculated phase-noise reduction is approximately 3.8 dB in the region. The measured phase-noise reduction from 100 kHz to 1 MHz is in agreement with the calculated phase-noise difference. In addition, the measured good 45-dB fundamental rejection for the second-harmonic self-injected push-push oscillator is because of the small amplitude mismatch (ΔA_O) of the fundamental signals for $V_R(t)$ and $V_L(t)$ and small

Fig. 8. Phase noise of the free-running push–push oscillator and the second-harmonic self-injected push–push oscillator with 45° total phase delay.

amplitude mismatch ($\Delta\hat{A}_1$) of the second harmonic signals for $V_R(t)$ and $V_L(t)$. From (30), the small amplitude mismatch ($\Delta\hat{A}_1$) of the second harmonic signals and the large second-harmonic oscillation amplitude ($\hat{A}_1$) are also the factors resulting in the low phase-noise oscillator. At the same bias condition, the output power is -16.5 dBm with a phase noise of -119 dBc/Hz at 1-MHz offset for the stable self-injected oscillator using a regular delay path and a circulator.

However, if the proposed oscillator is unstable when the total phase-delay ($\theta_f - \hat{\theta}_1$) shown in Fig. 2 approximates 170° not in the stable range described in (35), the measured phase noise of the unstable self-injected oscillator is -111 dBc/Hz at 1-MHz offset from the carrier. The phase noise degrades approximately 9.1 dB compared to that of the stable self-injected oscillator (-120.1 dBc/Hz at 1-MHz) with the same power consumption.

Fig. 9 shows the measured, simulated, and calculated phase noise at 1-MHz offset with respect to the total phase delay ($\theta_f - \hat{\theta}_1$) illustrated in Fig. 2 of the self-injected push–push oscillator. The simulation tool is Agilent's Advanced Design System (ADS), and the function blocks of the power splitter and phase shifter can be found in the "System-Passive" branch. The calculated phase noise in the $1/f^3$ region is obtained by estimating the phase-noise reduction with usage of the ISF. The measured, simulated, and calculated phase noises are better than -116.1 dBc/Hz of the free-running state. In region (I) of Fig. 9, the phase delay is from 0° to 90° satisfying the derived amplitude stability condition (16) and derived phase stability condition (20) simultaneously. The measured and simulated phase noises are both better than -116.1 dBc/Hz of the free-running state.

In region (II), the total phase delay is from 90° to 270° . These phase delays do not satisfy both the amplitude stability condition (16) and phase stability condition (20). The measured and simulated phase noise is worse than -116.1 dBc/Hz of the free-running state, and a worst -107.5 -dBc/Hz phase noise occurs at the total phase delay near 180° ($(2n+1)\pi$) in this region. These results can also be observed in Section II-C.2.

In region (III), the total phase delay is from 270° to 360° satisfying only the phase stability condition (20). The measured

Fig. 9. Measured, simulated, and calculated phase noise with respect to the total phase delays of the self-injected push–push oscillator.

Fig. 10. Measured output frequencies and output powers with respect to the supply voltages (V_{DD}) of the self-injected push–push oscillator.

and simulated phase noise is almost worse than that of the free-running state. The total phase delay including the probes, power splitter, delay-line cable, and tunable phase shifter are measured by using the HP8510 network analyzer.

While a 3-dB attenuator is inserted in the feedback loop to increase the amplitude-attenuation factor (K) defined in (30), the measured phase noise degrades 2.9 dB at 1-MHz offset in the stable self-injection state. When a 6-dB attenuator is inserted in the feedback loop, the phase noise degrades 5.1 dB at 1-MHz offset in the stable self-injected state. While increasing the transconductance (g_{m1}) of the current source by only raising its gate voltage, the oscillator phase noise improved up to 2.8 dB at 1-MHz offset in the stable self-injection state. These behaviors can be observed from the derived equations (30) and (31).

There is a 3-MHz oscillating frequency difference between the free-running state and the self-injected state under the same bias condition. This is due to the fact that the oscillator output loadings of these two cases are slightly different. Fig. 10 shows the measured output frequencies and output powers with respect to the supply voltages (V_{DD}) of the self-injected push–push oscillator. The frequency of the second-harmonic self-injected push–push oscillator is tuned by adjusting the supply voltages (V_{DD}). For the output power higher than -15 dBm, the tuning range is 97 MHz by adjusting the supply voltage (V_{DD}). While tuning the frequency, the total phase delay can be adjusted to the stable region ($2n\pi < \theta_f - \hat{\theta}_1 < (2n+1)\pi/2$) by tuning the phase shifter to keep low phase noise. The figure-of-merit described in (37) of the free-running push–push oscillator and the

TABLE III
PERFORMANCE SUMMARIES OF THE RECENTLY REPORTED SI-BASED OSCILLATORS AROUND 10 GHz WITH THIS STUDY

Process	Center Frequency (GHz)	Topology	Output Power (dBm)	Phase Noise (dBc/Hz)	Core Power Consumption (mW)	Supply Voltage (V)	Figure of Merit (dBc/Hz)	Ref.
0.18- μ m CMOS	10.2	Single Balance	-9	-114.8 at 1 MHz	15.7	1.8	-183	[30]
0.18- μ m CMOS	11	Transformer Feedback	> -21	-109 at 1 MHz	6.84	1.8	-182	[31]
0.18- μ m CMOS	9.83	Cross-Coupled Complementary	Not available	-89 at 0.1 MHz	5.8	1.8	-181.2	[32]
0.18- μ m CMOS	10	LC	-5	-105 at 1 MHz	7.2	1.8	-176.4	[33]
0.13- μ m CMOS	10	LC	Not available	-95 at 1 MHz	14.4	1.8	-163.4	[34]
0.18- μ m CMOS	9.39	LC	-26	-120 at 5 MHz	21.6	1.8	-172.2	[35]
0.13- μ m CMOS/SOI	10	LC	-18	-104 at 1 MHz	26	1.2	-169.8	[36]
0.18-μm CMOS	9.6	LC (without Self Injection)	-14	-116.1 at 1 MHz	13.8	1.0	-184.3	This Work free-running
0.18-μm CMOS	9.6	Regular Self Injection	-16.5	-119 at 1 MHz	13.8	1.0	-187.2	This Work with Circulator
0.18-μm CMOS	9.6	Proposed Second-Harmonic Self Injection	-14	-120.1 at 1 MHz	13.8	1.0	-188.3	This Work without Circulator

stable self-injected push–push oscillator are -184.3 and -188.3 dBc/Hz, respectively. Table III compares the recently reported Si-based oscillators around 10 GHz with this study. It is observed that the phase noise and figure-of-merit of the free-running push–push oscillator can be improved by using the proposed second-harmonic self-injection technique.

For the proposed second-harmonic self-injected push–push oscillator, with a higher transconductance (g_{m1}) of the current source, a higher feedback current ($I_f = g_{m1} \cdot V_f$) can be obtained. Increasing the feedback current (I_f) can improve the phase noise because of the increased oscillation amplitude (V_{inj}) crossing the tank ($V_{inj} = I_f \cdot R_{eq}$), where R_{eq} is the equivalent parallel resistance of the tank for the $2f_o$ self-injection signal. However, the phase-noise improvement will slow down when the tank amplitude (V_{inj}) approaches the oscillator supply voltage (V_{DD}) shown in Fig. 2.

Since the proposed self-injection topology does not require a circulator, it has the potential for integrating on a single chip in the future. The bias circuit can be implemented with a 4-pF on-chip bypass capacitor and a 5-nH on-chip miniature 3-D inductor [37] for the RF choke. In order to implement a single-chip self-injected push–push oscillator in the future, the delay path variation due to process variation has to be taken into account. An on-chip tunable delay line can be used to alleviate the path variation [38], but an additional process is required. In practical applications, the temperature-independent reference such as bandgap-reference circuits can be used to alleviate the temperature variation.

V. CONCLUSION

The design of the low phase-noise second-harmonic self-injected push–push oscillator has been presented. The low phase noise can be achieved when the total phase delay ($\theta_f - \hat{\theta}_1$) approximates to the stable region ($2n\pi < \theta_f - \hat{\theta}_1 < (2n + 1)\pi/2$). In addition, with higher transconductance (g_{m1}) of the current source, lower amplitude-attenuation factor (K) of the tunable delay path, smaller amplitude mismatch ($\Delta A_1(t)$) for the second-harmonic signals in $V_R(t)$ and $V_L(t)$, and larger second-harmonic oscillation amplitude (A_1), a better oscillator phase noise can be obtained. Moreover, using larger device gate area in the oscillator cross-coupled pair, a better oscillator phase noise and figure-of-merit can also be achieved. Furthermore, this second-harmonic self-injected push–push oscillator without a circulator or an amplifier in the feedback path can achieve low phase noise of -120.1 dBc/Hz at 1-MHz offset and good figure-of-merit of -188.3 dBc/Hz.

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To-Po Wang (S'05) was born in Hsinchu, Taiwan, R.O.C., in 1975. He received the B.S. degrees in mechanical engineering and in electrical engineering from National Sun Yat-Sen University, Taiwan, R.O.C., in 1998, the M.S. degree in communication engineering from National Chiao Tung University, Hsinchu, Taiwan, R.O.C., in 2000, and is currently working toward the Ph.D. degree at the Graduate Institute of Communication Engineering, National Taiwan University, Taipei, Taiwan, R.O.C.

From 2000 to 2003, he was with the BENQ Corporation, Taipei, Taiwan, R.O.C., where he was engaged in mobile phone research. His research interests are in the areas of RF and millimeter-wave integrated circuits (ICs) in CMOS, SiGe BiCMOS, and compound semiconductor technologies.

Zuo-Min Tsai (S'01) was born in Maoli, Taiwan, R.O.C., in 1979. He received the B.S. degree in electrical engineering and Ph.D. degree in communication engineering from National Taiwan University, Taipei, Taiwan, R.O.C., in 2001 and 2006, respectively.

His research interests are the theory of microwave circuits.

Kuo-Jung Sun was born in Tainan, Taiwan, R.O.C. He received the B.S. degree in electrical engineering from National Tsing Hua University, Hsinchu, Taiwan, R.O.C., in 1991, and the Masters degree in business and administration (MBA) and M.S. degree in communication engineering from National Taiwan University, Taipei, Taiwan, R.O.C., in 1997 and 2005, respectively.

His research interests include the design of RF integrated circuits (RFICs) and mixed-signal circuits.

Huei Wang (S'83–M'87–SM'95–F'06) was born in Tainan, Taiwan, R.O.C., on March 9, 1958. He received the B.S. degree in electrical engineering from National Taiwan University, Taipei, Taiwan, R.O.C., in 1980, and the M.S. and Ph.D. degrees in electrical engineering from Michigan State University, East Lansing, in 1984 and 1987, respectively.

During his graduate study, he was engaged in research on theoretical and numerical analysis of electromagnetic radiation and scattering problems. He was also involved in the development of mi-

crowave remote detecting/sensing systems. In 1987, he joined the Electronic Systems and Technology Division, TRW Inc. He has been an MTS and Staff Engineer responsible for monolithic-microwave integrated-circuit (MMIC) modeling of computer-aided design (CAD) tools, MMIC testing evaluation, and design, and then became the Senior Section Manager of the Millimeter-Wave Sensor Product Section, RF Product Center, TRW Inc. In 1993, he visited the Institute of Electronics, National Chiao-Tung University, Hsinchu, Taiwan, R.O.C., to teach MMIC-related topics. In 1994, he returned to TRW Inc. In February 1998, he joined the faculty of the Department of Electrical Engineering, National Taiwan University, as a Professor. He was elected the first Richard M. Hong Endowed Chair Professor of National Taiwan University in 2005.

Dr. Wang is a member of Phi Kappa Phi and Tau Beta Pi. He is a Distinguished Microwave Lecturer for the 2007–2009 term. He was the recipient of the Distinguished Research Award of the National Science Council, R.O.C. (2003–2006).