THERMAL LESION FORMATION AND DETERMINATION FOR EXTERNAL ULTRASOUND THERMAL THERAPY

HAO-LI LIU¹, YUNG-YAW CHEN¹, JIA-YUSH YEN² AND WIN-LI LIN³

¹Department of Electrical Engineering, ²Department of Mechanical Engineering,

³Institute of Biomedical Engineering, National Taiwan University
Taipei, Taiwan

ABSTRACT

The purpose of this paper is to investigate the relationship between the formation of the thermal lesion and the major parameters of the external ultrasound heating systems, and to propose a useful thermal lesion determination procedure, which is capable of specifying the range of a thermal lesion by temperature feedback in external ultrasound thermal therapy. This work is based on an ideal ultrasound power deposition formed by an external ultrasound heating system and the temperature distribution is calculated by the transient bioheat transfer equation. A simplified model was employed to determine the heating pattern for four most important parameters. Through the simplified power expression, the property of a new parameter, T_{300} , which is defined as the maximal temperature corresponding to the thermal dose of 300 minutes, is also investigated. When the target volume is large enough such that the thermal conduction effect becomes negligible, the T_{300} value is almost independent of the system parameters and the heating strategies, and is dominated by the blood perfusion rate with a monotonic correlation. The method enables us to use feedback information in the ultrasound heating process and to pre-determine the heating range of the thermal lesion, which will be very useful in ultrasound treatment planning.

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1. INTRODUCTION

The aim of ultrasound thermal therapy [1-5] is to use high intensity, short-duration, focused ultrasound [6-8] to deliver enough energy into a specific tumor volume such that tissue necrosis is formed and the overheating of the intervening normal tissue can be avoided [2,9]. The external ultrasound heating is a non-invasive and very flexible modality for heating deep-

seated tumors for its vast penetration and focusing ability. The major task in external ultrasound thermal therapy is to correctly form a thermal lesion on the targeted tumor volume. In practice, the thermal lesion cannot be visualized directly. Thermal dose distribution with a threshold value [10] is usually used to determine the effective region of thermal lesion.

The relationship between the size of the thermal lesion and the thermal dose distribution with threshold values has been studied in literatures. ter Haar et al. [27] performed high intensity, focused ultrasound trial in-vivo and exercised liver sample in-vitro to investigate the thermal lesion patterns under different sonication time and heating power. It was found that the thermal lesion enlarged with increasing sonication time and heating power. The conclusion was consistent

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Correspondence: Prof. Yung-Yaw Chen, Department of Electrical Engineering, National Taiwan University, No.1, Sec. 4, Roosevelt Road, Taipei, Taiwan 106
E-mail: yychen@cc.ee.ntu.edu.tw

with Hutchinson and Hynynen's [11] study for non-invasive ultrasound thermal therapy using phased arrays. Moreover, it was also found that a larger blood perfusion rate results in a smaller thermal lesion size in [2], while the shape as well as the size of the thermal lesion varies with different arrangement of external ultrasound heating systems [12].

Although there are many discussions on thermal lesion formation from the existing literatures, few studies focused on its relationship with the heating system arrangement, such as the size of the acoustic window, the focal depth, the attenuation coefficient and the size of the focal zone. These indices were found to be the major factors to form various power depositions and the associated heating patterns in external ultrasound heating systems. In addition, the determination of the sonication time and the heating power for a desired thermal lesion volume is difficult due to its complicated correlations to the above-mentioned system parameters.

The objectives of this research are to investigate the relationships between the formation of the thermal lesion and the major parameters of the external ultrasound heating systems, and to propose a procedure for thermal lesion formation and determination. Furthermore, the procedure will be shown to provide a proper and simple heating configuration for thermal therapy. In order to focus on the study to the parameters determinations in thermal lesion formation, the Specific Absorption Ratio (SAR) model is employed to approximate the absorbed power density generated by practical external ultrasound thermal therapy systems. The approach has been widely used and verified by many researchers in a number of experiments [13-15, 16,17]. The temperatures as well as the thermal dose distributions are calculated to examine the relationships between the system indices and the thermal lesion region, which is identified by a region with a threshold value of 300 minutes in thermal dose. Studies show that the heating temperature corresponding to a threshold value of thermal dose is only affected by the blood perfusion rate when the focal zone diameter is large than 2 cm. This property can be used in thermal lesion determination and consequently provides a guideline in thermal therapy design. Three design examples with different tumor volume settings are studied and both show satisfactory results on lesion determination. This paper provides a useful reference for researchers attempting to design the externally ultrasound thermal therapy system for deep-seated large tumors and offers a simple but useful clinical treatment lesion determination scheme.

2. MATERIALS AND METHDS

2.1 Specific Absorption Rate (SAR) Model

Fig. 1 shows the geometrical relationship between transducer and treatment portion in external ultrasound-heating model. The external ultrasound transducer is assumed to create an acoustic window of diameter $d(0)$ at the origin. The targeted tumor region is at distance Z_t with a diameter $d(Z_t)$. The z -axis is referred to be the depth of penetration and is vertical to the skin surface, which is located at the origin of the z -axis. The ultrasound wave is assumed to propagate in straight line, and to converge and focus on the targeted tumor region at $Z=Z_t$, and diverge beyond this focal depth. At $Z=0$ cm, the area with diameter $d(0)$ is referred to be the acoustic window of the ultrasonic beam. The deposition of ultrasonic intensity at each depth was considered to be a distribution symmetrical along the z -axis, i.e. the power deposition can be modeled to be two dimensional in the radial (R -axis) and the depth (Z -axis) directions. This arrangement provides a relatively simple but realistic approximation in evaluating the power deposition and the thermal dose distribution to avoid over-complicated calculations.

The ultrasonic power attenuates exponentially as it propagates through the tissue. Assuming that the ultrasonic power intensity is not too large to cause wave distortions and all the attenuated energy is absorbed by the tissue, the ultrasonic power at depth z cm, $Q(z)$, and the associated power intensity, $I(z)$, can be described by :

$$Q(z) = Q(0) \cdot e^{-2\mu \cdot z} \quad (1)$$

$$I(z) = \frac{Q(z)}{A(z)} \quad (2)$$

where $Q(0)$ is the total power propagating through the acoustic window, μ is the attenuation coefficient and $A(z)$ represents the cross-sectional area of the conical power region at depth z cm. From Fig. 1, it is clear that

$$A(z) = \pi [d(z)/2]^2 \quad (3)$$

$$d(z) = d(z_t) + (d(0) - d(z_t)) \cdot |z - z_t| / z_t \quad (4)$$

where $d(z)$ is the diameter of the conical power region at depth z cm. The acoustic attenuation coefficient μ depends on the driving frequency, and is approximately 5Np/m at 1MHz and 10Np/m at 2MHz [18].

The specific absorption rate (SAR) is defined to be the absorbed power density (q) in soft tissue, and can be calculated by:

Fig. 1 Schematic diagram of the geometry studied for the distribution of SAR ratio in the tissue for external ultrasound thermal therapy.

$$SAR(z) = 2 \alpha I(z) \quad (5)$$

where α is the absorption coefficient. Moreover, the SAR ratio (SR) between the SAR values at depth z and the focal depth z_t can be calculated as:

$$SR(z; z_t) = \frac{SAR(z)}{SAR(z_t)} = \frac{2\alpha I(z)}{2\alpha I(z_t)} = \frac{d^2(z_t)}{d^2(z)} \cdot e^{-2\mu(z-z_t)} \quad (6)$$

Once the SAR value at z_t is determined, the SAR value at depth z can be calculated by:

$$SAR(z) = SAR(z_t) \cdot \frac{d^2(z_t)}{d^2(z)} \cdot e^{-2\mu(z-z_t)} \quad (7)$$

In Eq. (7), the ratio of the cross-sectional areas between the focal zone at $z = z_t$ and the acoustic window at $z = 0$ (i.e. $d^2(z_t)/d^2(0)$) is defined to be the Geometrical Gain (GG) for the SAR model. The corresponding temperature distribution can be then computed from the $SAR(z)$ distributions in the following section.

2.2 Temperature and Thermal Dose Calculation

The tissue temperature response, T , is calculated using the well-known bio-heat transfer equation [19]:

$$\rho c_t \frac{\partial T}{\partial t} = k \nabla^2 T - w_b c_b (T - T_{ar}) + q \quad (3)$$

where c_t and c_b are the specific heats of tissue and blood (both set to be $3770 \text{ J/kg}^\circ\text{C}$), k is the thermal conductivity of tissue ($0.56 \text{ W/m}^\circ\text{C}$), w_b is the blood perfusion rate, and T_{ar} is the arterial blood temperature

(37°C). This equation is solved using a numerical finite difference method with all boundary and initial conditions set to 37°C . The time step and the grid spacing in the x -, y - and z -directions are 50 ms , 0.5 mm , 0.5 mm and 1 mm , respectively.

The thermal dose (TD), in terms of equivalent minutes at 43°C , is used to estimate the necrosed tissue volume, and is calculated using the following equation [10,20-22,24,25]:

$$TD = \int_{t_0}^{t_f} R^{(T-43)} dt \approx \sum_{t_0}^{t_f} R^{(T-43)} \Delta t \quad (4)$$

where $R = 2$ for $T \geq 43^\circ\text{C}$, $R = 4$ for $37^\circ\text{C} < T < 43^\circ\text{C}$, Δt is the time step, and t_0 and t_f represent the initial and the final times, respectively. The TD value required for total necrosis ranges from 25 to 240 minutes for brain to muscle tissues [8,24]. In this study, a value of $TD = 300$ minutes is chosen as the threshold for complete heating [26].

The absorbed power density at the focal depth in all five cases were set to be 16 W cm^{-3} with heating time of 6 seconds throughout the study unless otherwise mentioned. In our simulations, such transducer power will provide a maximal temperature about 60°C during the heating process. The computation of temperature profiles is terminated at time of 600s, which is sufficient to determine the TD distribution precisely. The SAR ratio distributions along the central z -axis with the parameter settings in Table 1 are shown in Fig. 2(a). The corresponding temperature distributions at the end of heating session (at $t = 6\text{s}$) and the thermal dose distributions (at $t = 600\text{s}$) are shown in Fig. 2(b) and Fig. 2(c) respectively. The maximal thermal dose with equal absorbed power density and heating time in five cases are different, which is caused by various thermal conduction effects from different SAR distributions. It can be observed that the maximal thermal dose is smaller if the SAR distribution has a sharper profile at the focal depth. The cross-sectional areas with TD value 300 minutes in Fig. 2(c) for five cases in Table 1 are different. Their dimensions increase as μ (Case 1 vs. Case 4) and z_t (Case vs. Case 2) increases and as geometrical gain (Case 1 vs. Case 3 and 5) decreases. It is also found that to deliver the same absorbed power density to heat the focal zone with diameter $d(z_t)$ cm at focal depth z_t cm, the propagated ultrasound power attenuate more seriously and more ultrasound power will be absorbed in front of the treatment target then cause the pre-focal overheating. To prevent this, the acoustic window ($d(0)$) can be enlarged to an appropriate geometrical gain setting (Lin et al., 1999).

2.3 Thermal Lesion Determination Using T_{300}

Table 1. The focal depth (Z_f), focal zone diameter ($d(Z_f)$), acoustical attenuation (μ) and acoustic window ($d(0)$) settings studied for the distributions of SAR ratio and the resulting temperature and thermal dose (case 1 is regarded as a typical setting).

Case	Z_f (cm)	$d(Z_f)$ (cm)	μ (Np/m)	$d(0)$ (cm)
1	10	2	5	10
2	15	2	5	10
3	10	2	5	10
4	10	4	15	10
5	10	2	5	7

The temperature at the end of the ultrasound heating always corresponds to the maximum value in the temperature profile and seems to be related to the thermal dose values. It is, therefore, possible to determine the range of thermal lesion from temperature observations. The temperature distribution within the target volume will increase as the transducer continuously providing the energy and reach its maximum profile at the time the heating is terminated. The corresponding maximum temperature at this point is then defined to be the temperature of thermal dose value 300 minutes and is denoted by T_{300} . The observation of T_{300} can simply follow the arrow line between Figure 2(b) and 2(c). For all the five cases discussed in Table 1, the value of T_{300} is about 51°C both in the pre-focal and post-focal regions and seems to be insensitive to the variation of parameters. The value of T_{300} along the central z-axis is shown in Figure 2(a)-(c). Fig. 2(d) shows the r-z temperature distribution of case 1 at the end of heating (6 seconds), and the dashed line represents the computed thermal dose contour of TD value 300 minutes. Possible factors to T_{300} value include system parameter, blood perfusion rate, absorbed power density, heating rate, and absorbed power density. This will be analyzed in Sec. 3.1 and 3.2.

3. RESULTS

3.1 Effect of Different System Parameters

In this analysis, the typical values of the four systems parameters Z_f , $d(Z_f)$, μ , and $d(0)$ are set to be 10 cm, 2 cm, 5 Np/m and 10 cm, respectively. The four parameters are solely altered to individually examine the effects the T_{300} value, and the corresponding thermal doses are shown in Fig. 3. From this figure, it can be observed that the size of the TD = 300 min. contour increases with μ and Z_f . The observed T_{300}

Fig. 2 (a) The SAR ratio distributions with the parameter setting listed in Table 1, (b) heating temperature distributions at the time heating power is turned off (6s) and (c) thermal dose distributions when the parameters in Table 1 is used. Dashed lines in (b) and (c) represent the TD = 300 minutes and temperature at 51°C, respectively. (d) shows the temperature distribution in the transverse plane when the heating power is turned off (parameter settings of case 1 in Table 1 is used). Dashed contour represents the resulting thermal dose with 300 minutes.

Fig. 3 Thermal dose distributions along central z-axis at (a) Z_f is set to 5/10/15/20 cm, (b) $d(Z_f)$ is set to 1/2/3/4 cm, (c) μ is set to 2.5/5/10/15 Np/m and (d) $d(0)$ is set to 5/7.5/10/12.5cm when the other parameters are set to case 1 in Table 1.

value are found ranging from 51.1°C to 51.3 °C except for the case of small $d(z_f)$. The exception seems to be from the small focal zone diameter, which causes the value of T_{300} along the central z-axis easily affected by thermal conduction effect.

3.2 Effect of Different Blood Perfusion Rates and Absorbed Power Densities

Blood perfusion rate (W_b) is also a critical factor affecting the thermal dose distribution and the contour of T_{300} . For illustrations, different blood perfusion rates of 0.5/2/5/10/20 kg/m³/s and $d(z_f)$ of 0.5/1.0/1.5/2/3/4 cm were selected to depict the various conditions of human body. The corresponding T_{300} values in the pre-focal area on the central z-axis are shown in Fig. 4. It can be found that T_{300} decreased monotonically with increasing $d(z_f)$, and converged to steady values with $d(z_f)$ larger than 2 to 3 cm. The values of T_{300} with the blood perfusion rates of 0.5, 2, 5, 10, 20 kg/m³/s converged to 49.2°C, 51.2°C, 52.7°C, 53.8°C and 54.8°C, respectively. It is reasonable that higher blood perfusion rate acts as a strong heat sink, and takes the energy away faster. The result is higher temperature elevation required to achieve the thermal dose threshold of 300 minutes, which means the value of T_{300} is higher.

When $d(z_f)$ is smaller than 2cm, the corned-shape power profile at the focal depth z_f is narrower, and hence the value of T_{300} is affected by both the blood perfusion rate and thermal conduction effect. On the other hand, When the focal zone diameter $d(z_f)$ is large enough (approximately 2 cm in diameter), the T_{300} is dominantly affected by the blood perfusion rate, and the thermal conduction effect can be neglected.

The absorbed power density is also an important factor for T_{300} values. With constant heating time (6s in our examples), higher power intensity setting provides

Fig. 4 Relationship between T_{300} and the focal region diameter $d(z_f)$ when the blood perfusion varies from 0.5 to 20 kg/m³/s.

a higher temperature elevation, which results in higher peak values in thermal dose distributions and bigger thermal lesions. Fig. 5(a) and Fig. 5(b) show the relationships between T_{300} and different values of absorbed power density with constant heating time, different blood perfusion rates, and $d(z_f)$ of 0.5 cm and 2 cm respectively. The value of T_{300} decreased monotonically with increasing absorbed power density as shown in Fig. 5(a), while the T_{300} values showed no apparent changes as the absorbed power intensity varied in Fig. 5(b). The difference between Fig. 5(a) and 5(b) is from the size of $d(z_f)$. Similar to the conclusion above, the conduction effect is strong when $d(z_f)$ is small, while the blood perfusion rate becomes dominant when $d(z_f)$ is large enough.

The corresponding thermal dose distributions with the power density of 18 and 38 W/cm³ and the blood perfusion rates of 0.5 and 20 kg/m³/s are shown in Fig. 5(c) with $d(z_f)$ of 0.5 cm and in Fig. 5(d) with $d(z_f)$ of 2cm. It was found that the thermal dose distributions changed when the absorbed power density or blood perfusion are different. The absorbed power density had a greater influence to the thermal dose distributions than the blood perfusion rate. We also found that with smaller $d(z_f)$ and smaller power density, diameter of the induced necrosis volume decreases and T_{300} increases from the thermal conduction effect.

3.3 Effect of Different Heating Rates

In real thermal therapies, different heating strategies are usually determined heuristically. The heating strategy in our paper is referred to the determination of heating power level and heating time. Even for constant energy settings (i.e., constant product of heating power and heating time), different heating temperature patterns and thermal lesions are usually formed. In this section, the values of T_{300} under different heating strategies are discussed and listed in Table 2. It is found that T_{300} values maintain consistent results under different heating strategies with the same blood perfusion rate.

3.4 Thermal Lesion Determination Procedure

According to the above analysis, it is concluded that the value of T_{300} is only determined by the blood perfusion rate when $d(z_f)$ is larger than 2 cm. The property can be used to perform thermal lesion coverage determination by controlling the temperature of the selected target points to reach the proper T_{300} value. To determine the thermal lesion dimension, at first, two target points on the heating volume's boundary are set, one is ahead and the other is behind. Next, it is only to design the heating pattern, which can

Fig. 5 Relationship between T_{300} and the absorbed power density at focal depth when the blood perfusion rate is varied from 0.5 to 20 kg/m³/s and $d(Z_f)$ is set to (a) 0.5 cm and (b) 2 cm. (c) and (d) depict the respective thermal lesions under different absorbed power density (18 and 38 W/cm³) and blood perfusion (0.5 and 20 kg/m³/s) under $d(Z_f)$ is set to (c) 0.5 cm and (d) 2 cm.

deliver the same absorbed power density level onto these two target points and heat until reach the value of T_{300} . The overall thermal lesion determination procedure is as follows:

1. Determine z_f and $d(Z_f)$ to completely cover the target tumor. Moreover, according to the transducer and the driving frequency, the m and $d(0)$ and be also determined. Here, the treatment volume must be larger than 2cm in diameter to be eligible for our approach.
2. The front and rear boundaries of the target volume along the central z-axis are defined as the front target and rear target points.
3. Apply the simplified SAR model to roughly estimate the power deposition. Note that since the selected pair (z_f , $d(0)$) is not unique, therefore, a suitable z_f and $d(0)$ should be determined to offer enough geometrical gain (GG). A GG value larger than 10 is suggested to prevent the thermal lesion extension problem.
4. With the given blood perfusion of the tissue, determine the value of T_{300} according to Fig. 6.
5. Choose a heating power of the ultrasound thermal therapy system, which can offer the maximal absorbed power density over 20W/cm³ (according to the result shown in Fig. 5(b)).

Table 2. T_{300} under different heating strategies and different blood perfusion rates (2,5 and 10 kg m⁻³ s⁻¹).

Case	q (W/cm ³)	Heating time (s)	W_b (kg/m ³ /s)	T_{300} (°C)
1	20	5	2	51.1
2	10	10	2	51.1
3	10	15	2	51.0
4	20	5	5	52.5
5	10	10	5	52.5
6	10	15	5	52.6
7	20	5	10	53.6
8	10	10	10	53.6
9	10	15	10	53.5

6. Start heating the target volume using the determined power distribution. Turn off the heating power when the temperature at the front target point reaches T_{300} . Note that the treatment time will be shorter if the heating power chose in step 6 is larger.

7. Finally, the cumulative thermal dose distribution will roughly fit the target volume.

3.5 Control Examples

In order to show the validity of our thermal therapy design procedures, three cases with various tumor sizes are illustrated in the following section. In all three cases, the shape of the tumor is assumed to be of the cylindrical type.

In the first case, the cylindrical type treatment region with 2-cm wide, 2-cm thickness at the depth of 7 cm was assumed. The tumor diameter $d(Z_f)$ is set to be 2cm, and z_f , $d(0)$ and m were selected to be 7.5 cm, 8 cm and 10 Np/m, respectively. The resulting geometrical gain is 16, which is large enough to provide an appropriate geometric relation. The tissue property is assumed to be the same as in the previous cases except the blood perfusion was set to be 2 kg/m³/s. In order to evaluate the validity of using T_{300} information for performing the thermal therapy under different heating strategies, the maximal absorbed power density were set to be 2 W/cm³ and 32 W/cm³ respectively. T_{300} was determined to be 51.2°C according to Fig. 5. The front and rear target points are selected from the SAR distribution along the central z-axis according to the above-mentioned procedure, where the SAR distribution can be found from the calculation of equation 6 and 7. The heating power was turned off when the temperature of the front target

point reached the set T_{300} value, and the heating time on 2 W/cm^3 and 32 W/cm^3 were 52.6s and 3.2s, and The r-z thermal dose distributions are shown in Fig. 6(a) and 6(b). The contours with 1, 10, 100 and 300 minutes were plotted using real lines, and the regions enclosed by the dashed lines represent the region with the absorbed power densities larger than the power at the front and the rear target points. From Fig. 6, it shows that the thermal lesion coverage generated by different heating strategies is different. Thermal lesion formed by lower power density is smaller, which is due to the thermal conduct effect under the longer treatment time. However, the effect is not very significant to the central portion of the heating volume and the thermal lesion regions in both cases are pretty good results.

At second, a case of small tumor ($d(Z_i) < 2\text{cm}$) is shown with a cylindrical type treatment region of 1 cm in width, 1 cm in thickness and 7.5 cm in depth. The rest of the parameters are the same as the above case. The heating times on 2 W/cm^3 and 32 W/cm^3 are 62.7s and 3.8s, and the respective thermal lesions are formed and shown in Fig. 7(a) and 7(b). It indicates that, since the heating volume is not large enough, the temperature on the target points are strongly affected, and the thermal lesions cannot be correctly determined.

The third case shows a cylindrical type treatment region with 3-cm wide, 3-cm thickness and 7-cm depth was assumed. In order to show the effect of the acoustic window $d(0)$ on the coverage of the thermal lesion, $d(0)$ is set to be 10 cm and 14 cm, which provides geometrical gains of 11.1 and 21.8 respectively. The maximal absorbed power densities are both set to be 16 W cm^{-3} , and other parameter settings are identical to above cases. The SAR ratio distributions are shown in Fig. 8(a). In order to fit the

Fig. 6 Thermal dose distributions of the designed SAR ratio with the maximal absorbed power density set to (a) 2 and (b) 32 W/cm^3 under $d(Z_i) = 2 \text{ cm}$. The dashed lines are the regions with the absorbed power densities larger than the power on the two target points. Dots on the contours represent the “front target point” and “back target point” respectively in each figure.

Fig. 7 Thermal dose distributions of the designed SAR ratio with the maximal absorbed power density set to (a) 2 and (b) 32 W/cm^3 under $d(Z_i) = 1 \text{ cm}$.

SAR ratio curve to form a 3-cm thickness region correctly, the selected positions of target points for both cases are slightly different. The heating times are 6.45s when $d(0) = 10 \text{ cm}$, and 9.4s when $d(0) = 14 \text{ cm}$. After heating the target points to the pre-determined T_{300} value, the formed thermal lesions are shown in Fig. 8(b) and 8(c), respectively, with successful thermal lesion determination results.

4. DISCUSSION

In this paper, a useful thermal lesion determination procedure is proposed, which is capable of specifying the range of a thermal lesion by temperature feedback in external ultrasound thermal therapy. The method enables us to use feedback information in the ultrasound heating process and to pre-determine the heating range of the thermal lesion, which will be very useful in ultrasound treatment planning.

In this analysis, the SAR model is used to determine the parameters in the ultrasound heating setup, and provides a relatively simple expression of power deposition with four most important parameters. Through the simplified power expression, the property of a new parameter, T_{300} can be observed. Specifically, when the target volume is large enough (with $d(Z_i)$ larger than 2cm) such that the thermal conduction effect becomes negligible, T_{300} defined on the central z axis is almost independent of the system parameters ($d(0)$, Z_i , μ) and the heating strategies (different absorbed power density setting and heating time), and is dominated by the blood perfusion rate with a monotonic correlation.

Based on the observations, two target points associated with the T_{300} are selected and used for temperature feedback. Simulations show that the thermal lesions resulted from our heating procedure can be accurately determined and bounded by the two defined target points along central z axis and the size of $d(Z_i)$ along radial axis, and is almost independent of

Fig. 8 (a) the designed SAR ratio distributions with $d(0)=10$ and 14 cm . (b) and (c) are the respective thermal dose distributions, while the absorbed power densities are both set to 16 W/cm^3 .

different combination of heating strategies.

In clinical treatment, our thermal lesion determination procedure will be quite useful, since it provides a feedback configuration that gives a more reliable therapeutic session and enhances the treatment quality. Moreover, independency to different heating strategies of the procedure will reduce the necessity of precise power control in practical system operations.

5. CONCLUSION

In conclusion, a thermal lesion determination scheme is proposed to offer an easy but useful guideline to precisely heat the selected deep-seated tumors. The key factor, T_{300} in the proposed scheme, is only affected by blood perfusion rate while the heating volume is large enough. This strategy provides a simple implementation to perform "on-line feedback" control in ultrasound thermal therapy.

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